

# Microstructural Characterization: Application to Granular Cohesion

IFPRI Cohesion Workshop, January 2020

**Ryan C. Hurley<sup>1</sup>**

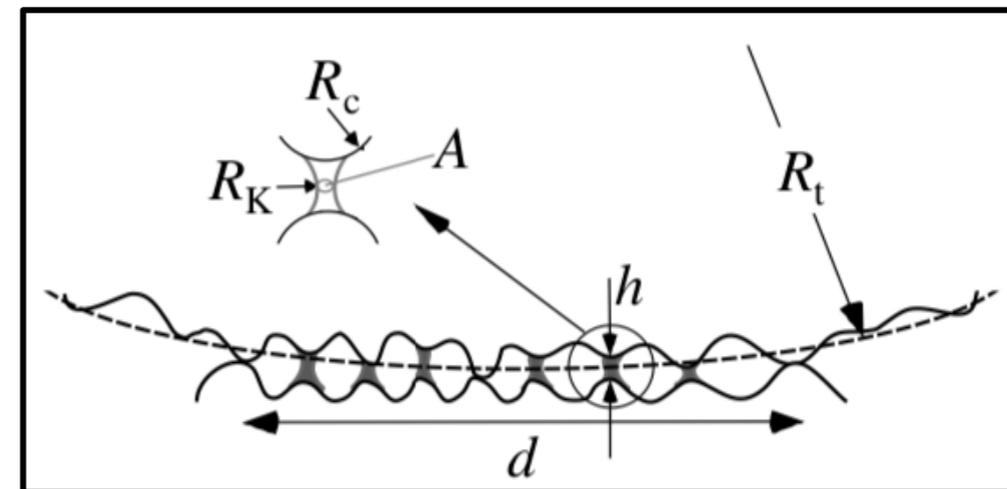
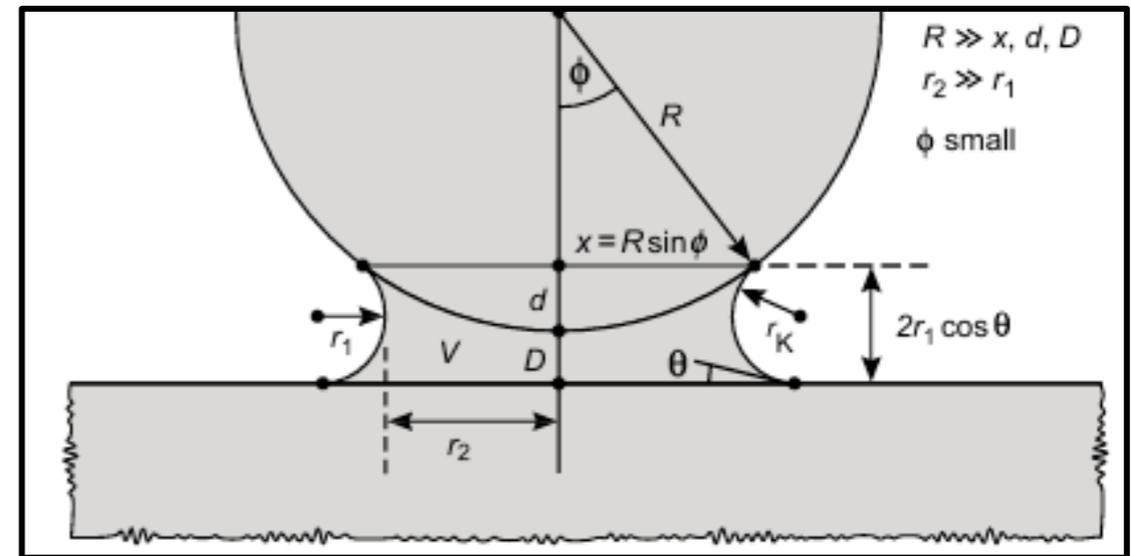
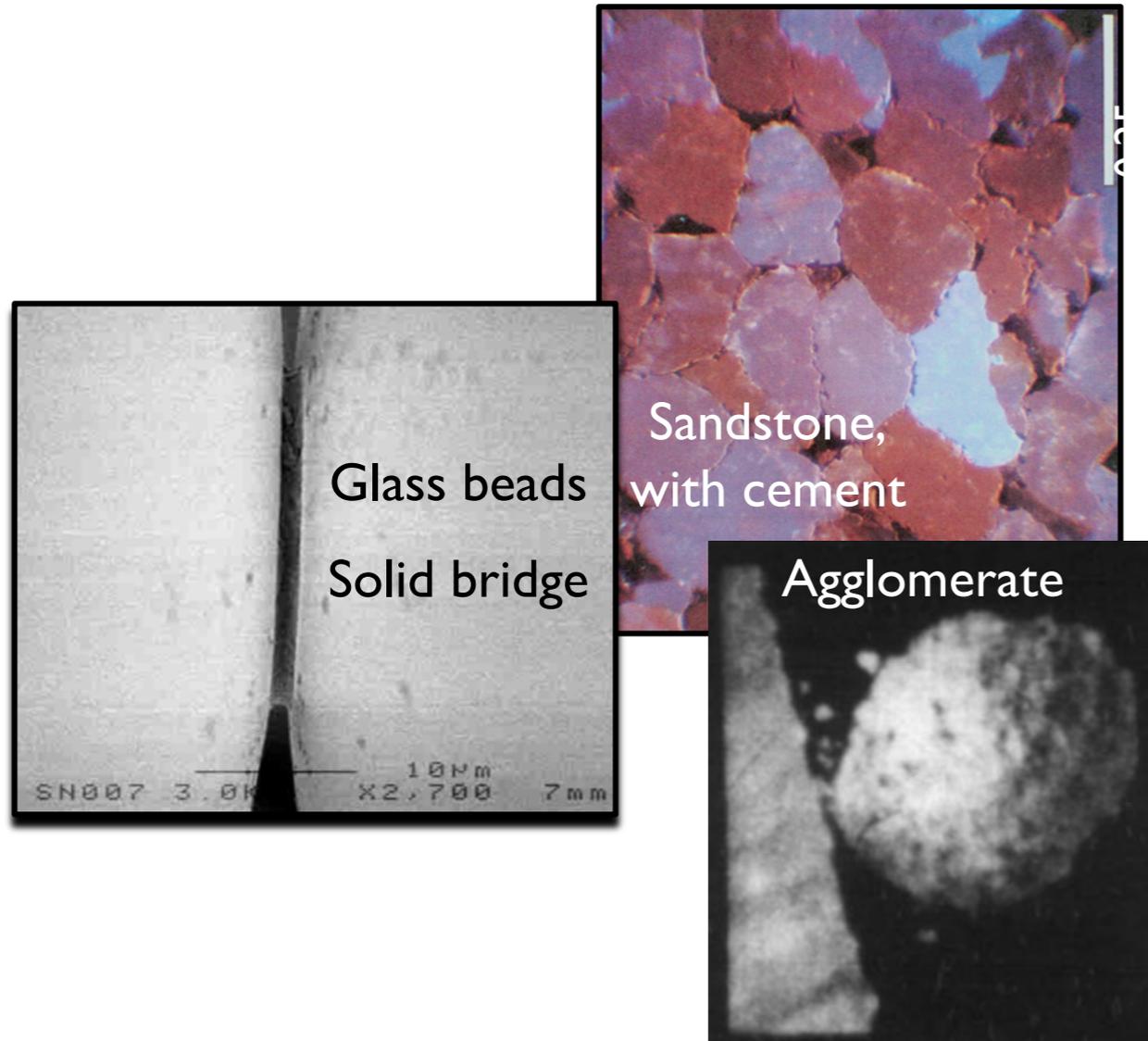
<sup>1</sup>Mechanical Engineering, Hopkins Extreme Materials Institute, Johns Hopkins University





# Motivation

(1) Cohesion mechanisms of interest? (2) What are our relevant microscale characterization techniques at bulk, particle levels?



Cementation: geology (diagnosis), engineering (bio-cementing), tableting

[Houseknecht, AAPG, 1987.; Olivi-Tran, et al., *Eur. Phys. J. B*, 2002.; Mullier, et al., *Pow. Tech.*, 1991.]

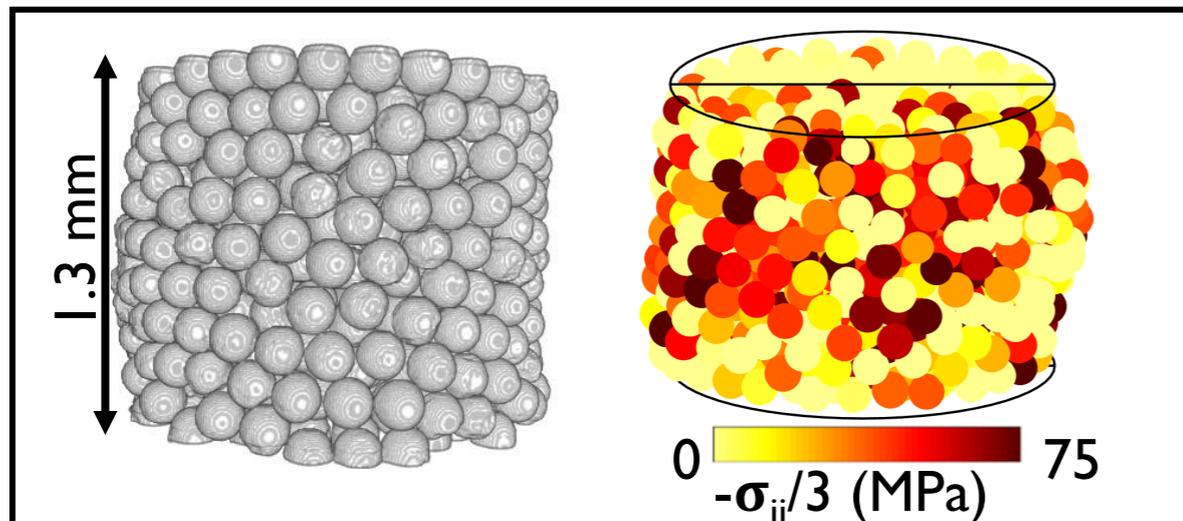
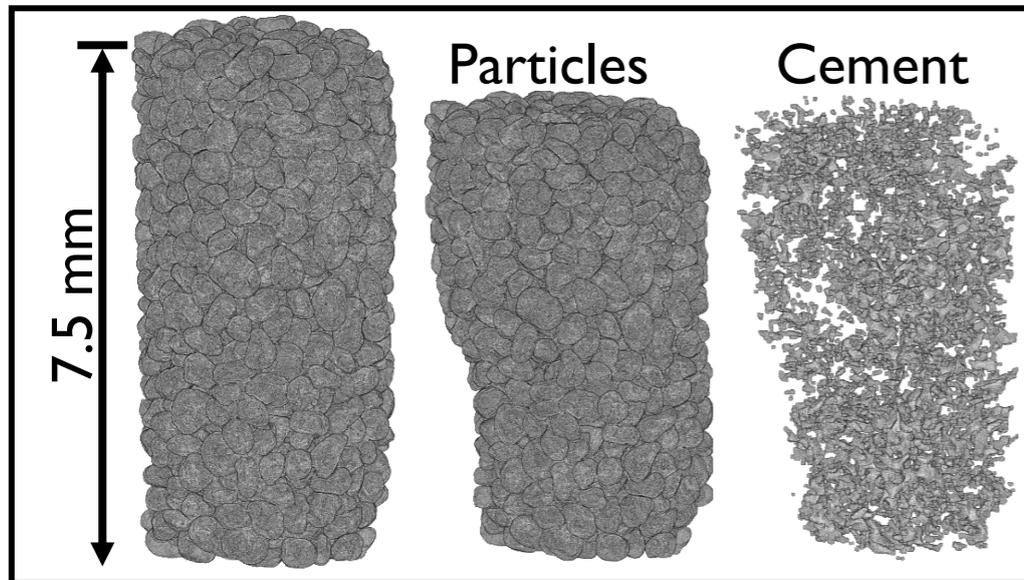
Capillary condensation: aging/adhesion of any rough surfaces in humid environments

[Israelichveli, 2011. Bocquet, et al, *Nature*, 1998.]

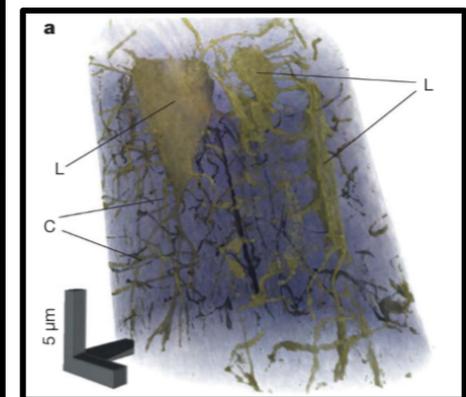
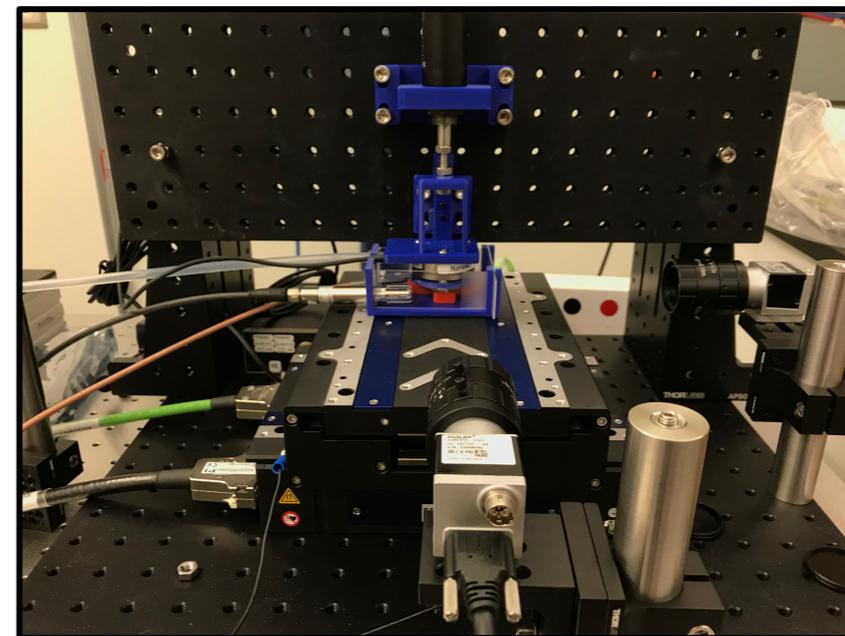
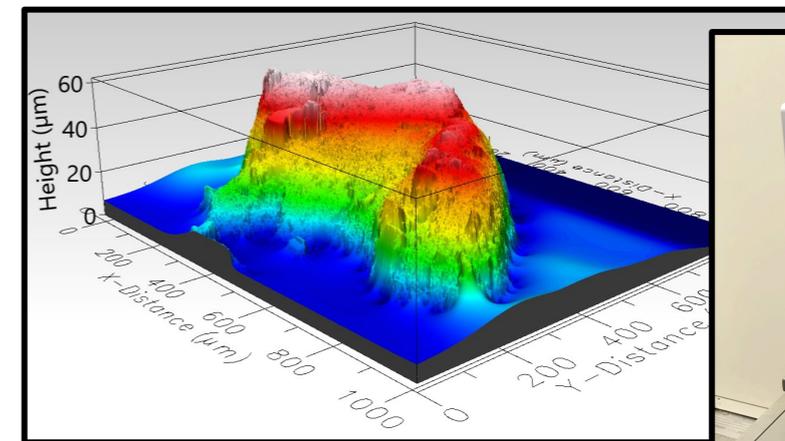


# Motivation

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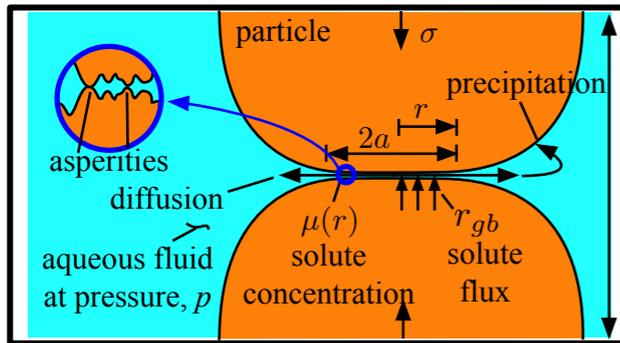


Micro, bulk: *in-situ* laboratory X-ray tomography, *in-situ* synchrotron 3D X-ray tomography, diffraction  
[Zhai, et al., JOM, 2020. Zhai & Hurley, unpublished.]

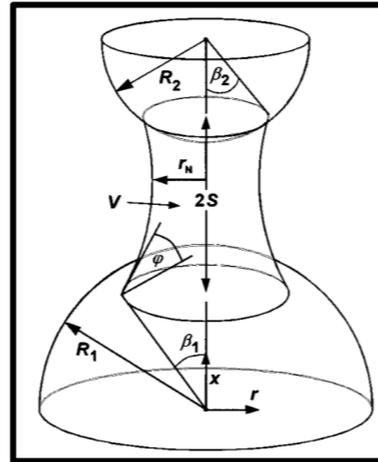


Micro, particle: surface profilometry, *in-situ* contact mechanics testing, *in-situ* 3D X-ray nanotomography  
[Hurley lab at JHU.; Dierolf, et al. Nature, 2010.]

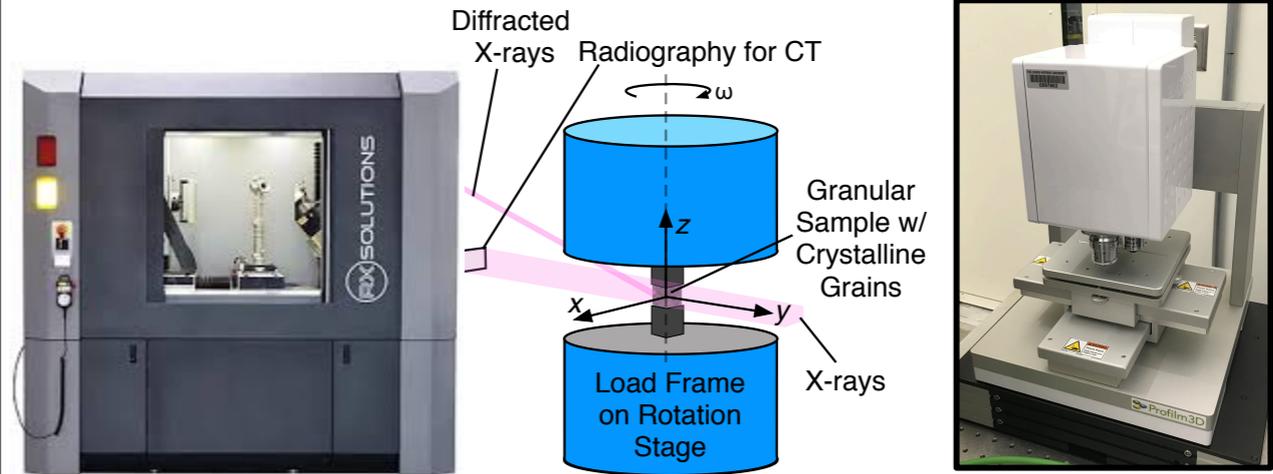
# Outline



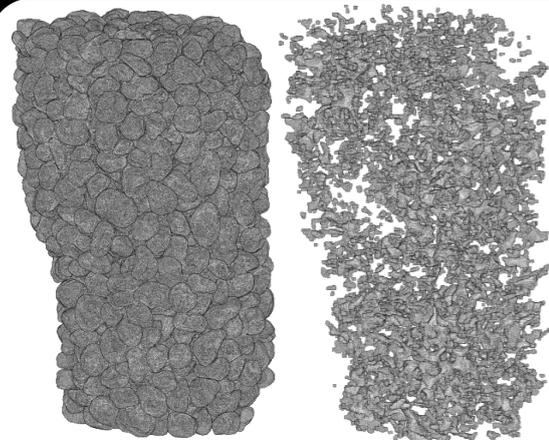
Inter-particle cementation



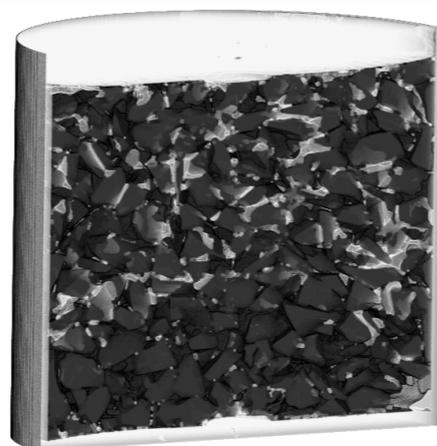
Capillary condensation



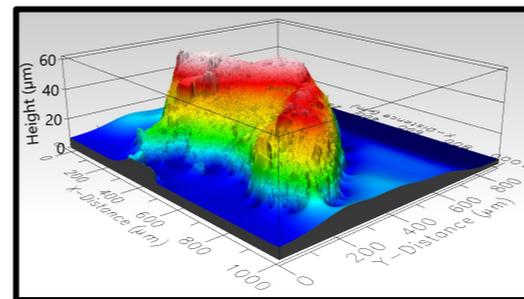
2. Characterization Tools



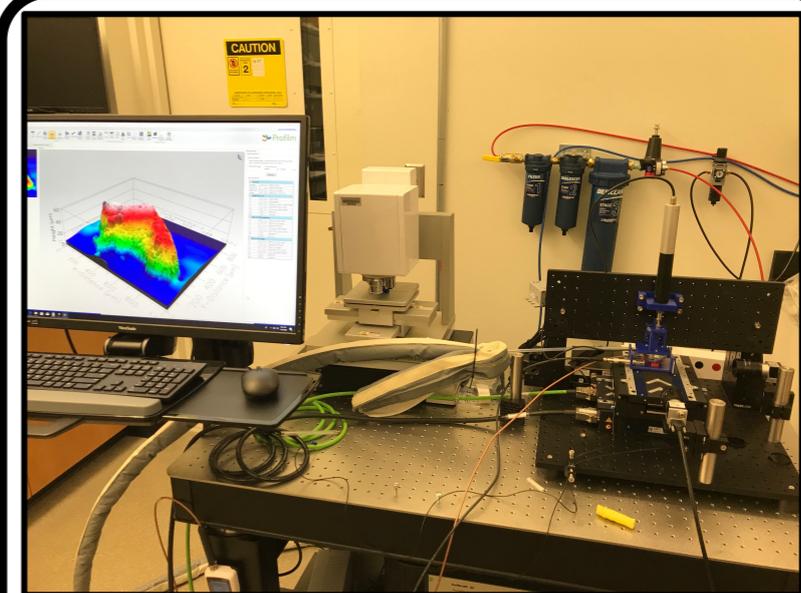
(1) XRCT: cemented cohesive mechanics



(2) XRCT + 3DXRD: particle-level stresses



(3) Roughness, %RH effects on particle-scale interactions



4. Summary, Goals

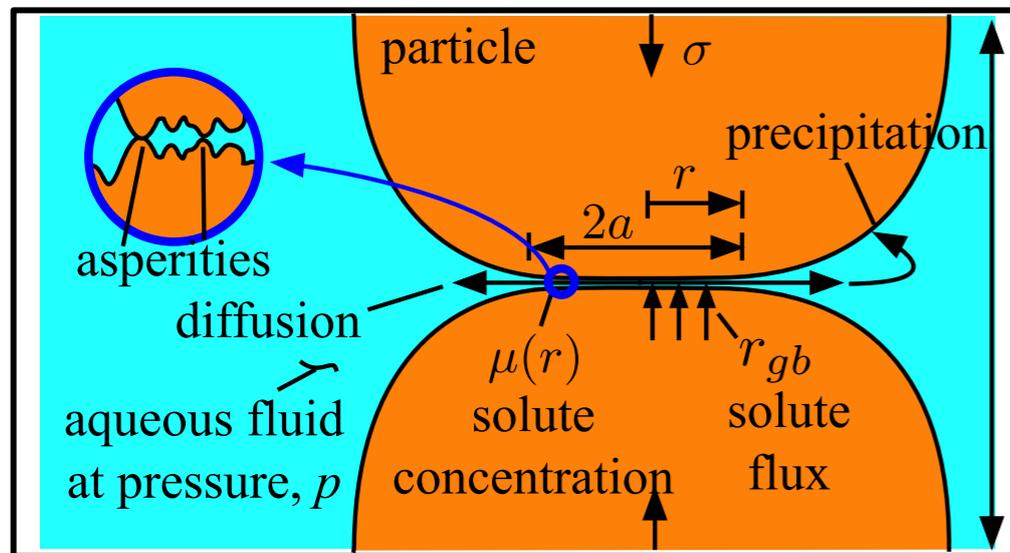
1. Mechanisms, Challenges

3. Past & Future Applications

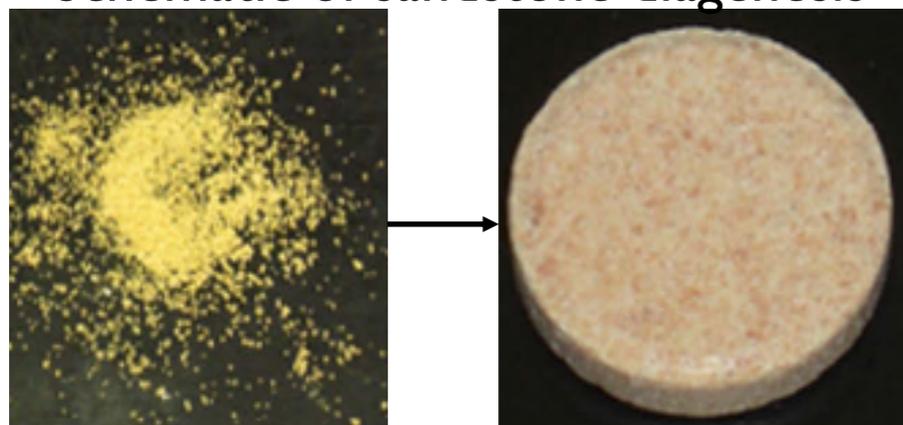
# I. Mechanisms, Challenges



I. Cementation: chemical or physical sintering of inter-particle contacts, found in geology and industry

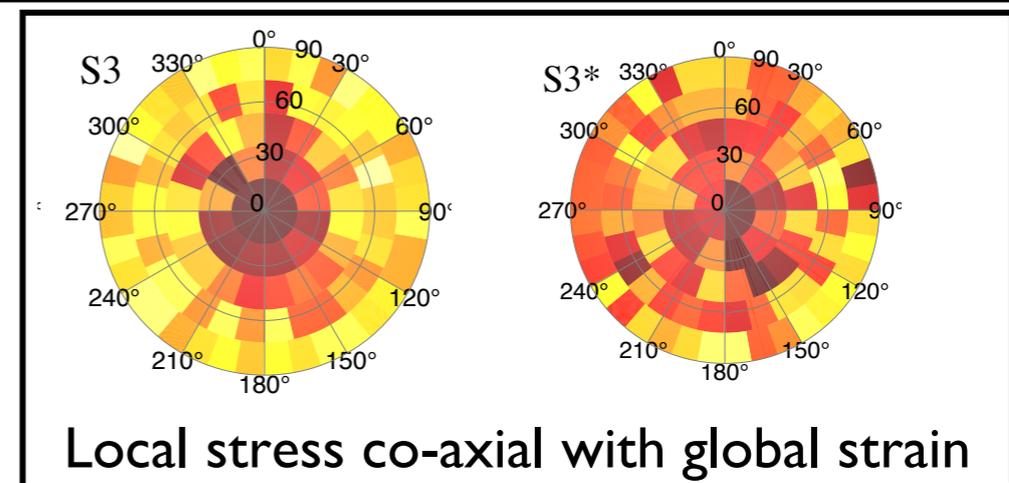
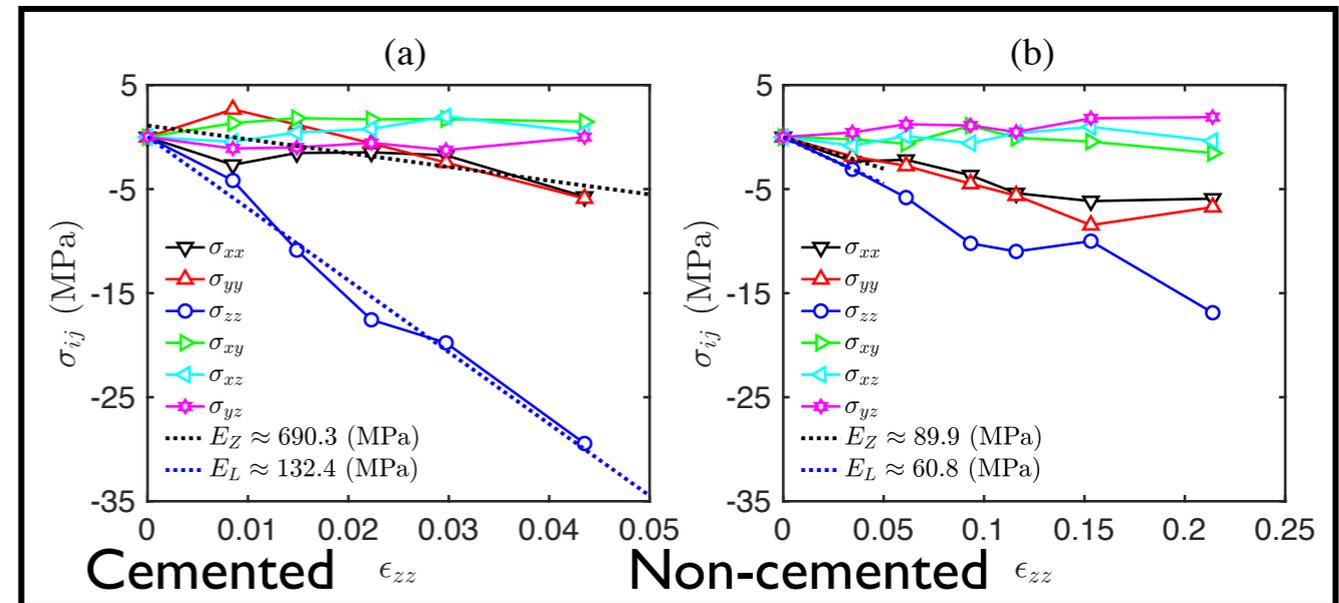


Schematic of sandstone diagenesis



Tablet formation

Causes: Natural & synthetic reactions, polymer binders for agglomeration, tableting  
 [Hurley, unpublished.; Lehner & Leroy, *Int. Geophys. Ser.*, 2004. Alanazi, *S. Pharm. J.* 2010.]



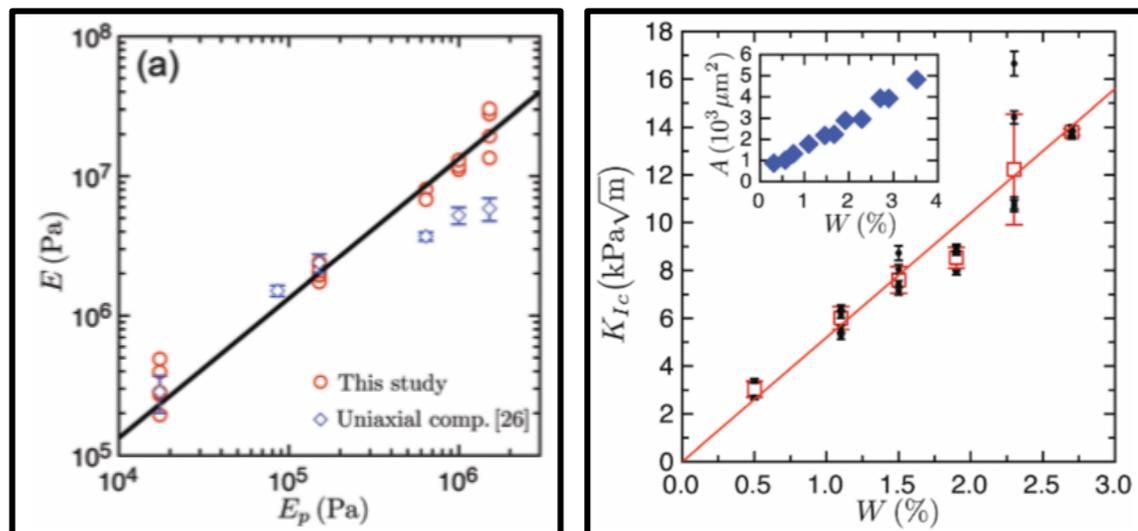
Local stress co-axial with global strain

Effects: Porosity (bulk), kinematics (particle), strength & coaxiality increase (both), fracture changes (both)  
 [Zhai, et al., *JOM* 2020 & unpublished.;.]



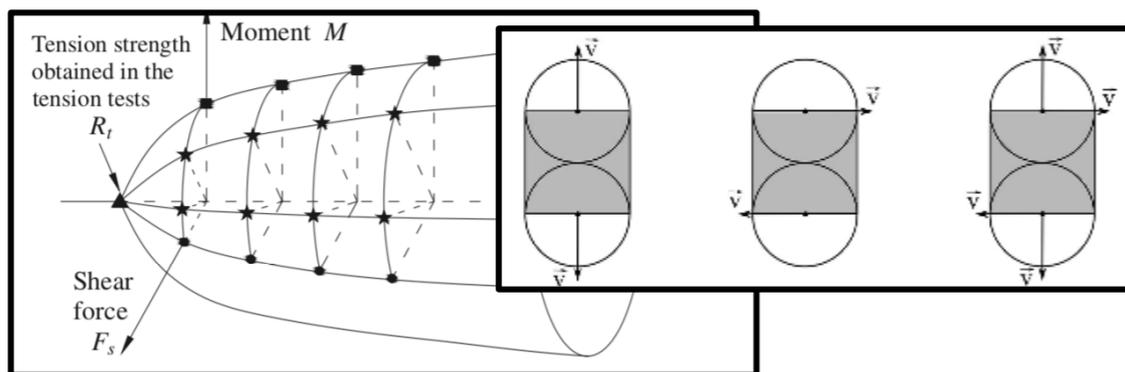
# I. Mechanisms, Challenges

I. Cementation, challenges: (1) Link particle/binder props. and bulk elastic ( $E$ ,  $\nu$ ) and fracture ( $K$ ,  $G$ ) properties? (2) Particle/contact-scale fracture/fragmentation modes? (3) Non-uniform strain/stress fields?

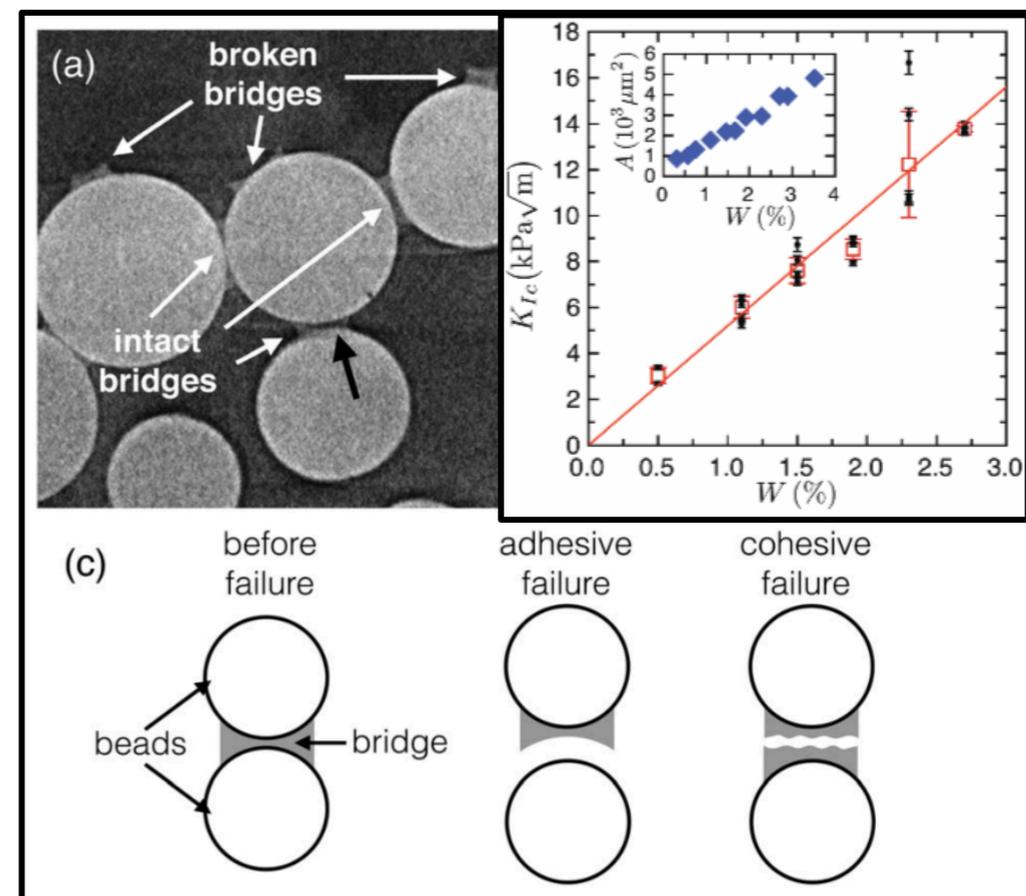


Elasticity scaling:  $E \propto A$ ,  $E \propto E_p$

[Hemmerle, et al., *Sci. Rep.* 2016.]



Theoretical/2D exps. for fracture modes [Nguyen, et al. *IJP*, 2017.; Jiang, et al., *MoM*, 2012.]



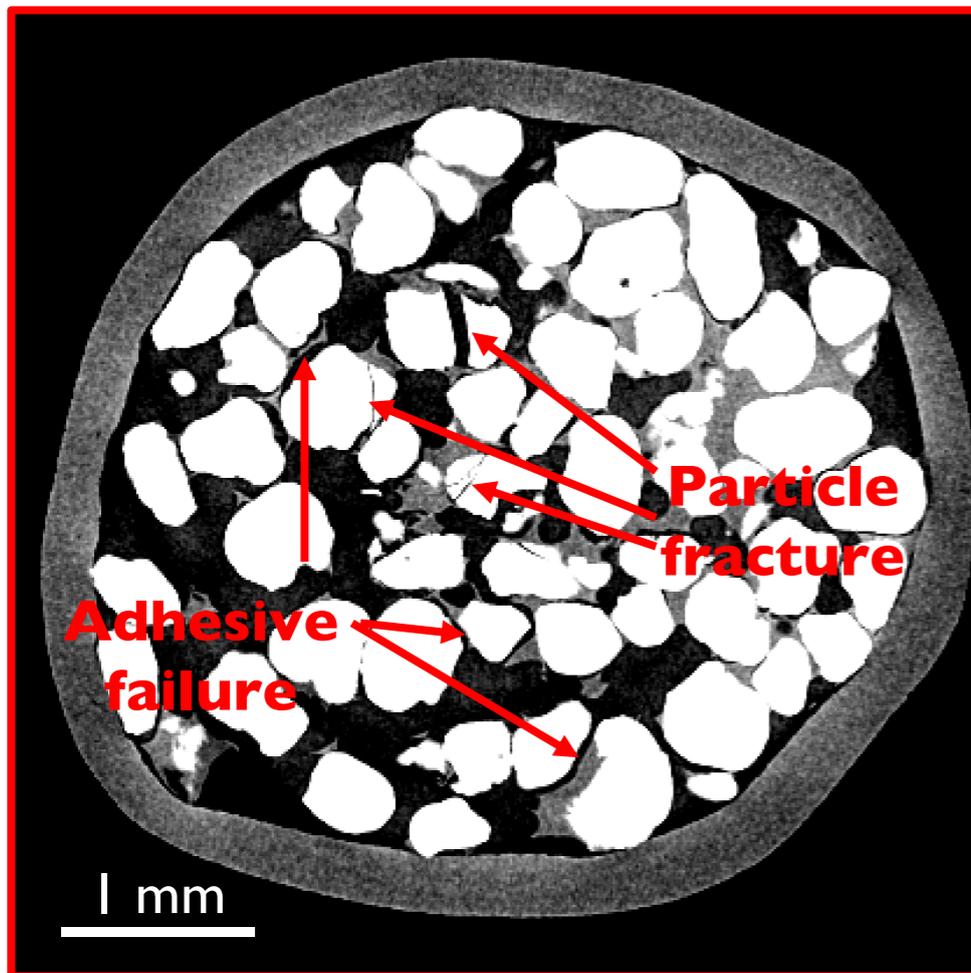
Fracture scaling:  $K_{IC} \propto \phi_p$ ,  $G \propto A$   
 $K = \sqrt{(GE)} \rightarrow K \propto A$

Fracture modes: bridge detachment, some plasticity [Schmeink, et al. *Soft Matter*, 2017.]

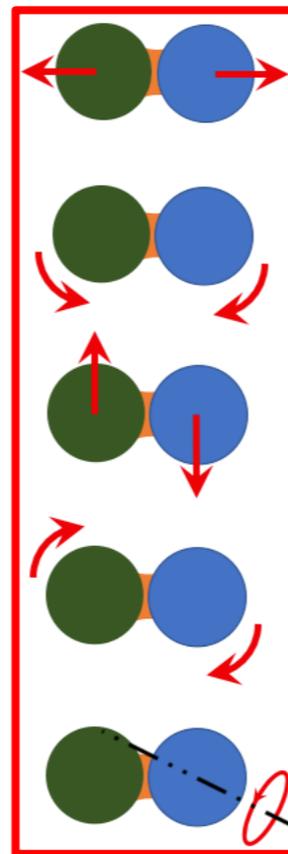


# I. Mechanisms, Challenges

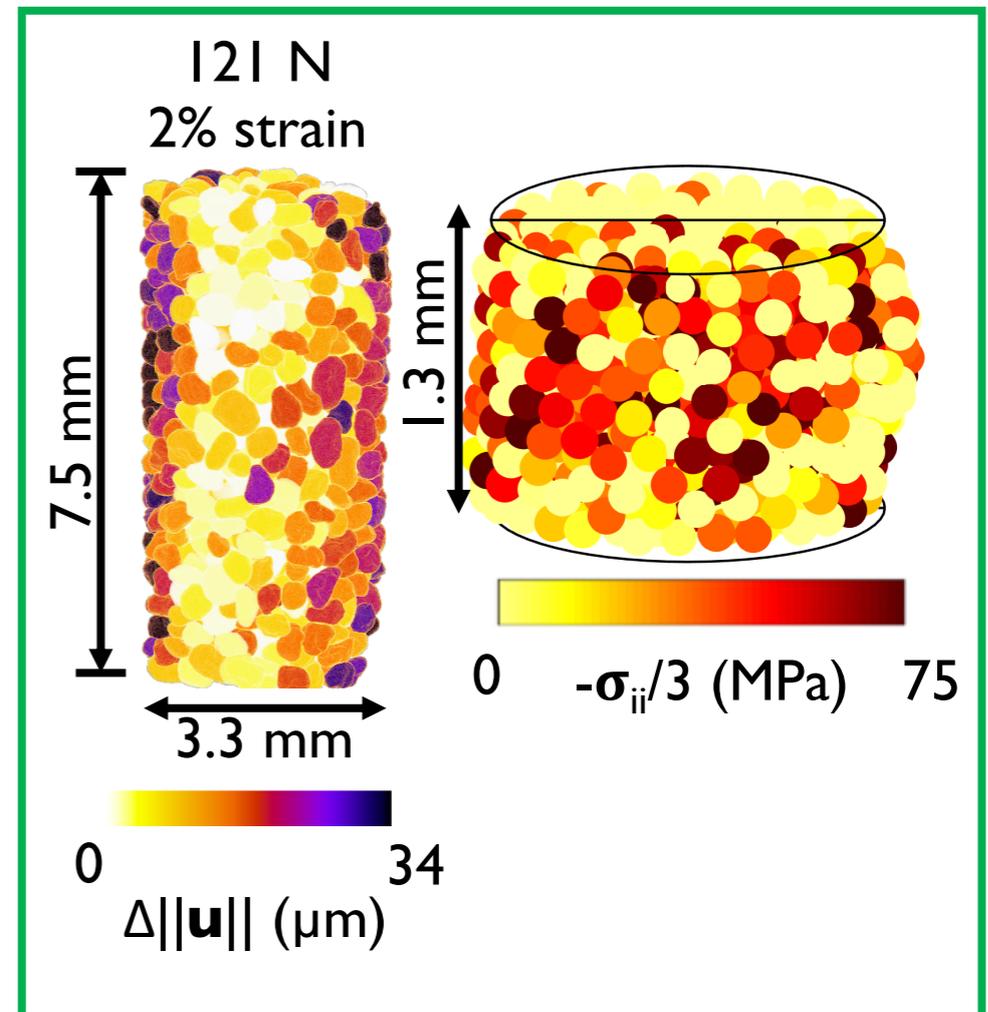
I. Cementation, challenges: (1) Link particle/binder props. and bulk elastic ( $E, \nu$ ) and fracture ( $K, G$ ) properties? (2) Particle/contact-scale fracture/fragmentation modes? (3) Non-uniform strain/stress fields?



Ottawa sand



Is adhesion-failure always strength-limiting?



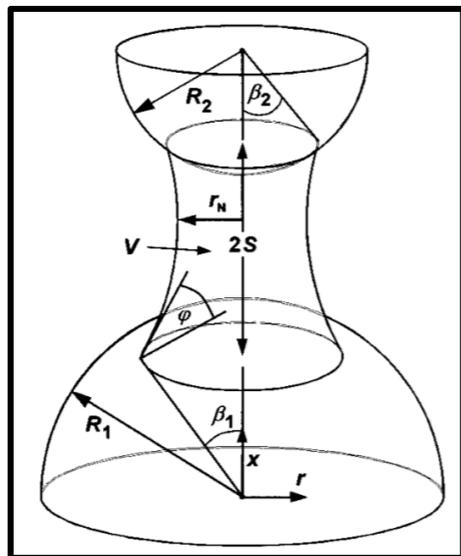
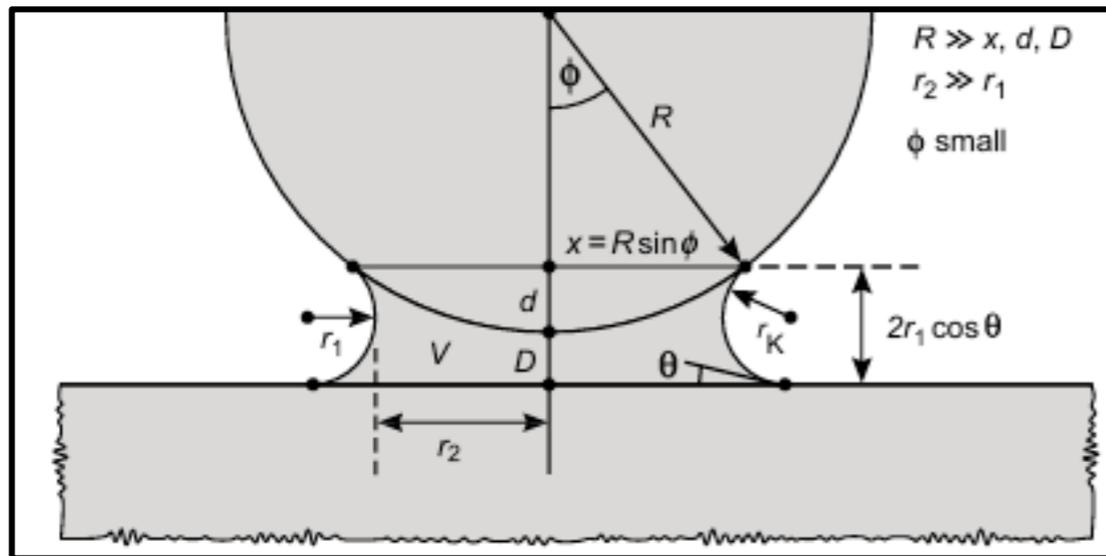
Most recent work focuses on the case when particle-binder adhesion is limiting. **Other fracture modes?**

Most experiments assume uniform strain fields. **Other mechanical loading, non-uniform strain and stress fields, *in-situ* monitoring?**

# I. Mechanisms, Challenges

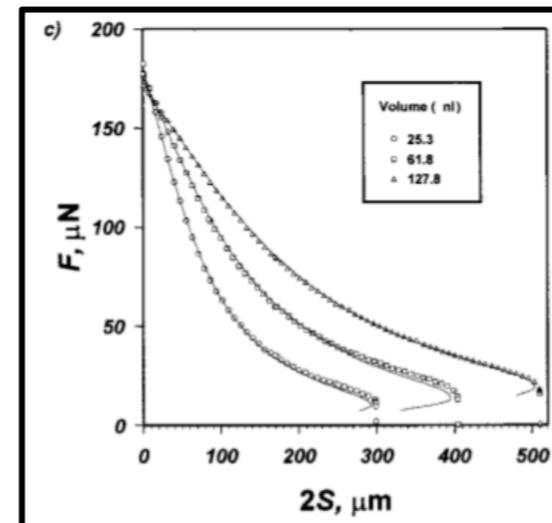
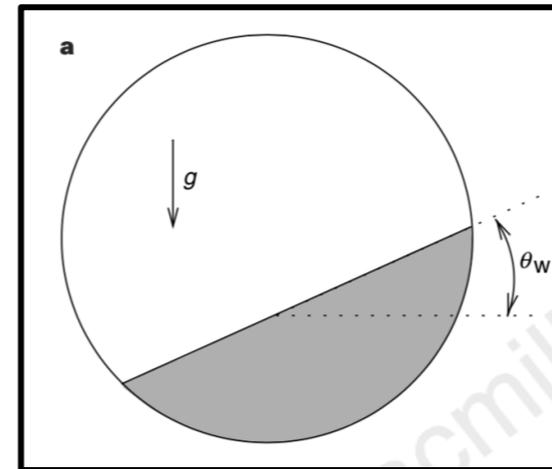


## 2. Condensation/humidity mechanism: capillary bridges in pores and contact throats due to reduction in vapor pressure

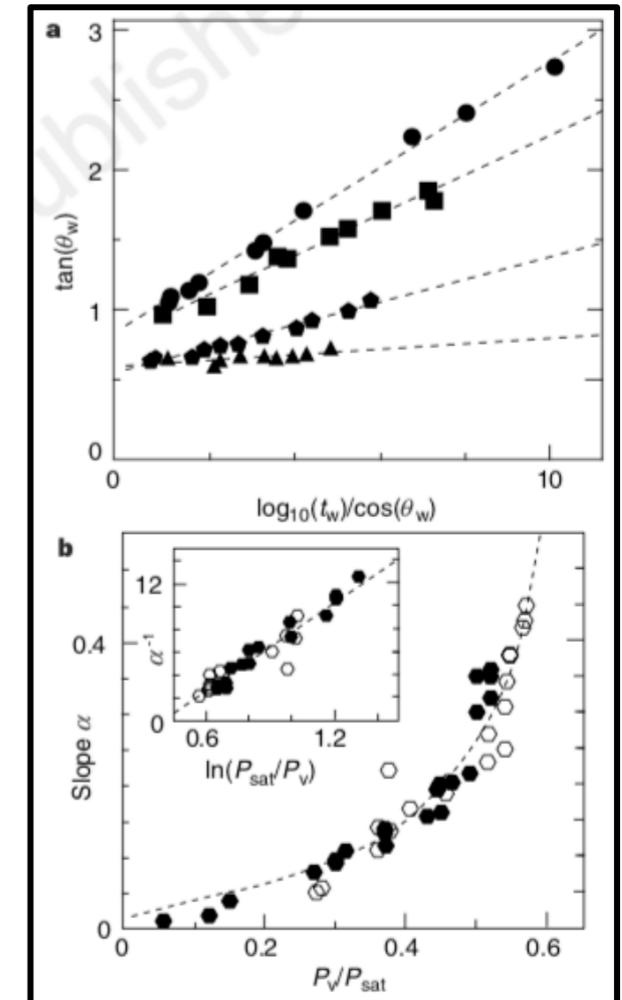


$$F_{ad} = 2\pi r \gamma + \pi r^2 \Delta P$$

Causes: Condensation in narrow spaces, favorable due to reduction in vapor pressure [Israelichveli, 2011. Willet, et al. *Langmuir*, 2000.]



Adhesion as a function of bridge volume



Logarithmic friction aging, friction vs. humidity

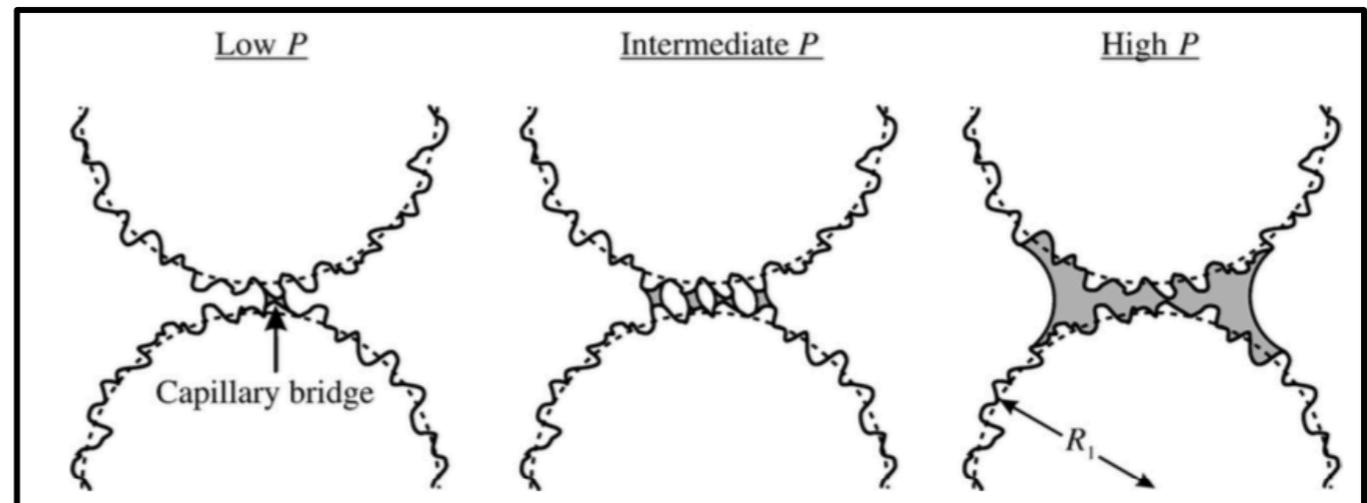
Effects: Adhesion (particle-scale), enhanced friction & viscosity (bulk scale), logarithmic aging (both scales) [Israelichveli, 2011. Willet, et al. *Langmuir*, 2000. Thornton, et al., *J. Phys.D*, 1996. Bocquet, et al., *Nature*, 1998.]

# I. Mechanisms, Challenges



2. Condensation/humidity challenges: (I) Adhesion and friction forces as a function of humidity & roughness at both contact- and bulk scales?

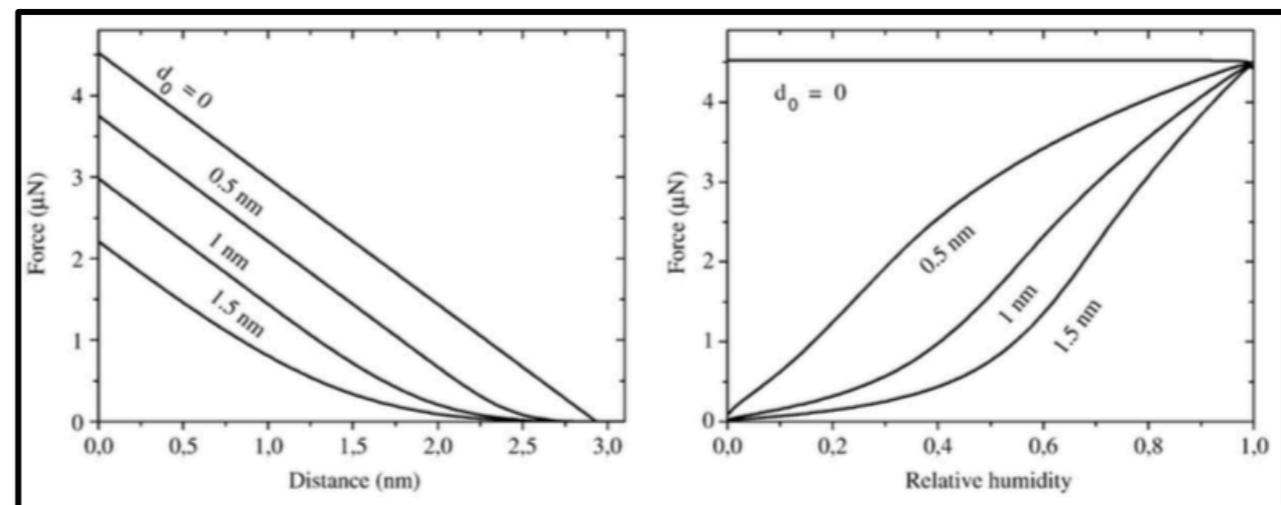
$$F_{\text{ad}} = \frac{AR}{6H_0^2} \left[ \frac{1}{1 + \left(\frac{32Rk_{1\text{rms}}}{\lambda^2}\right)} + \frac{1}{\left(1 + \frac{k_{1\text{rms}}}{H_0}\right)^2} \right]$$



$$f_A \sim \frac{\Gamma V_1}{l_R^2} \left(\frac{V}{V_1}\right)^{(2-\chi)/(2+\chi)}, \quad \text{for } V < V_1$$

$$f_A \sim \frac{\Gamma V}{l_R^2}, \quad \text{for } V_1 < V < V_2$$

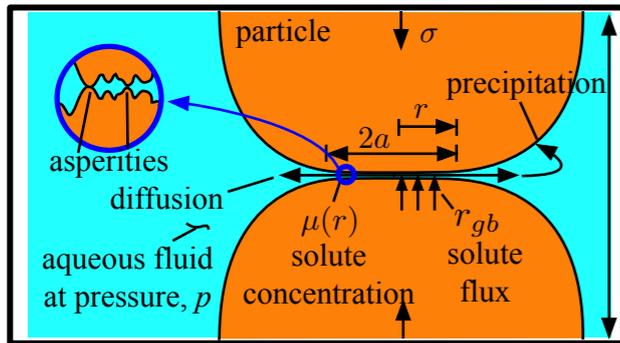
$$f_A = 2\pi\Gamma R, \quad \text{for } V > V_2$$



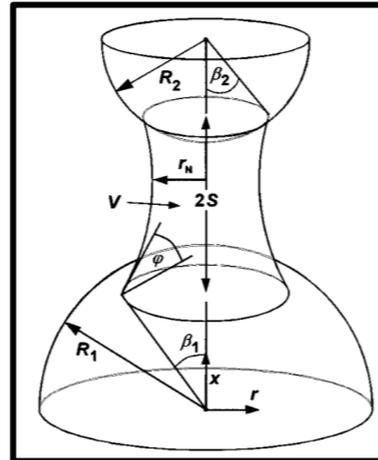
Roughness can reduce adhesion forces & separation distances/strains for rupture:  
[Rabinovitch, et al., *J. Coll. & Int. Sci.* 2000.]

Roughness leads to three regimes of capillary adhesion, changes force vs humidity profile  
[Butt and Kappl, *Adv. Coll. & Int. Sci.*, 2009.]

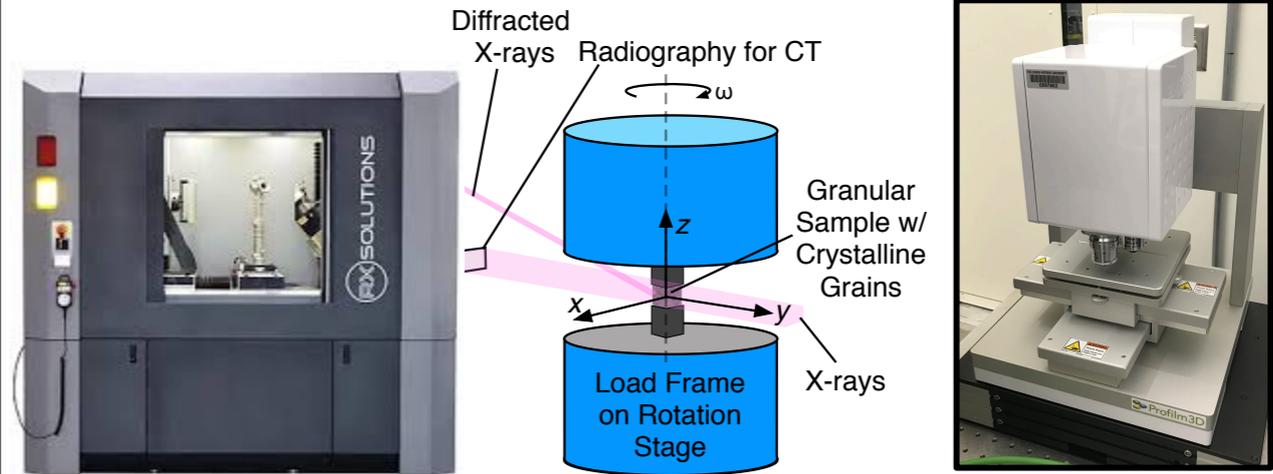
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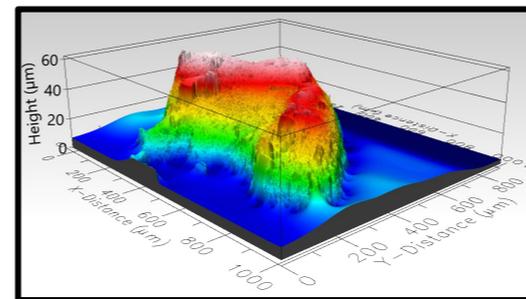
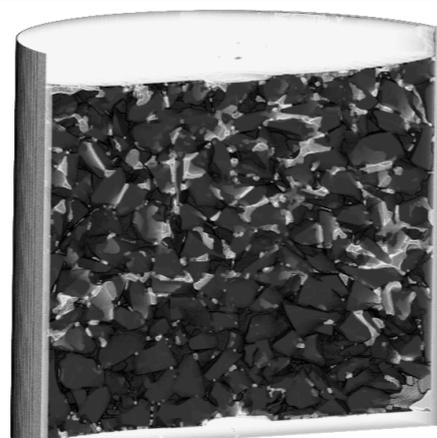
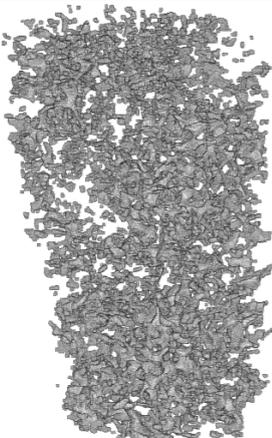
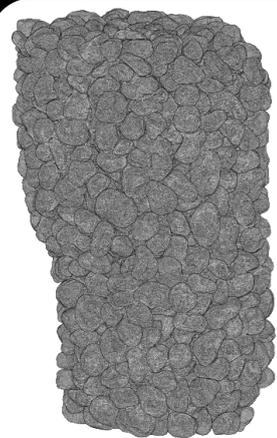
Inter-particle cementation



Capillary condensation



2. Characterization Tools

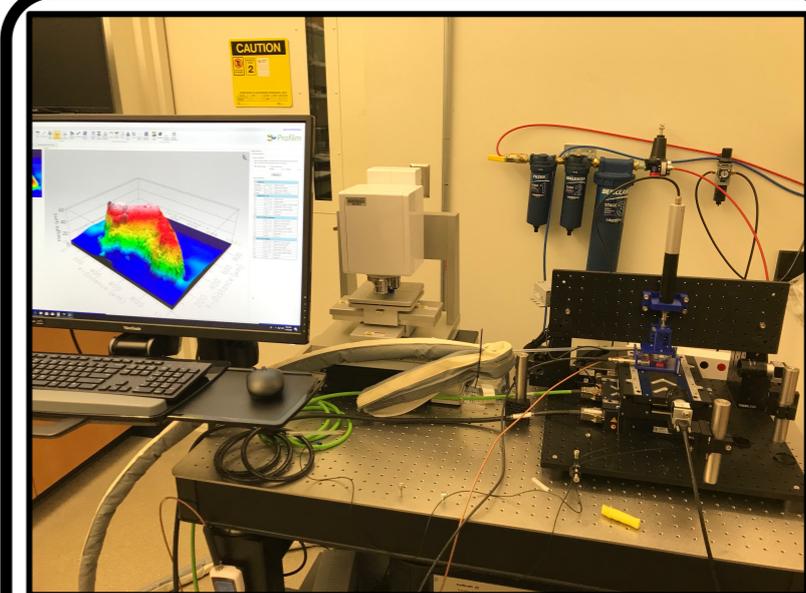


(3) Roughness, %RH effects on particle-scale interactions

(1) XRCT: cemented cohesive mechanics

(2) XRCT + 3DXRD: particle-level stresses

3. Past & Future Applications



4. Summary, Goals

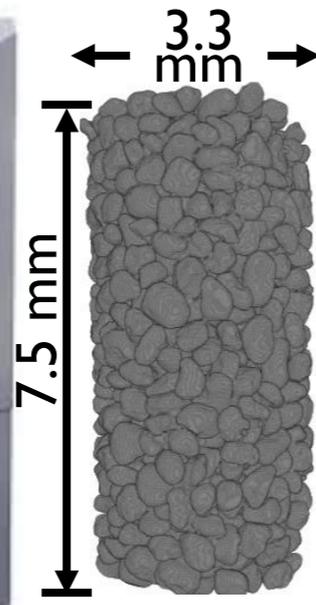


# 2. Characterization Tools

1. In-situ laboratory X-ray computed tomography (XRCT).
2. In-situ synchrotron XRCT and 3D X-ray diffraction (3DXRD).
3. Surface profilometry & friction/contact/adhesion testing.



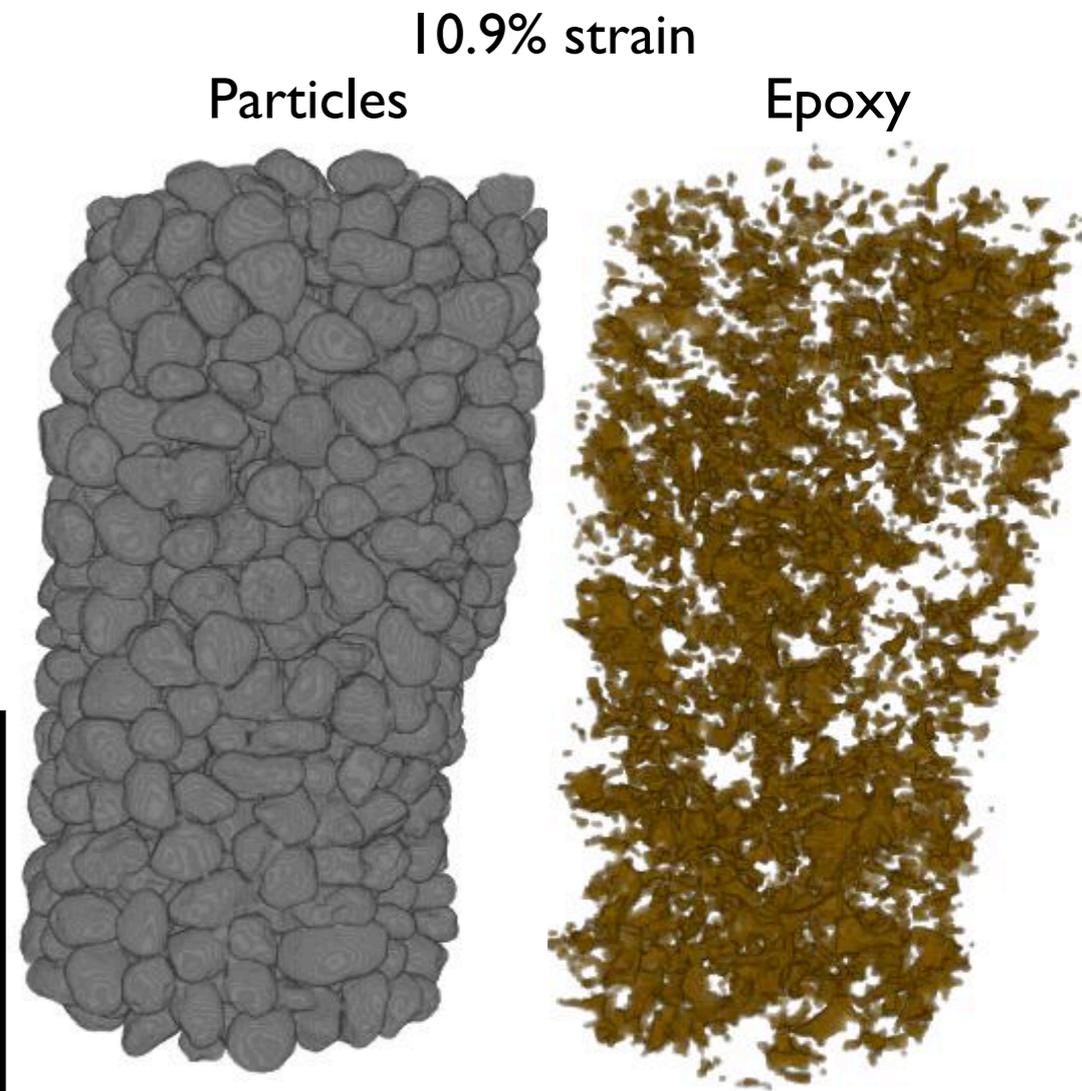
RX Solutions Easytom I60



Sample



X-ray radiographs



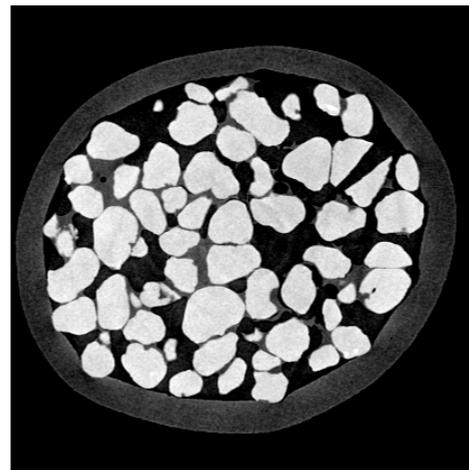
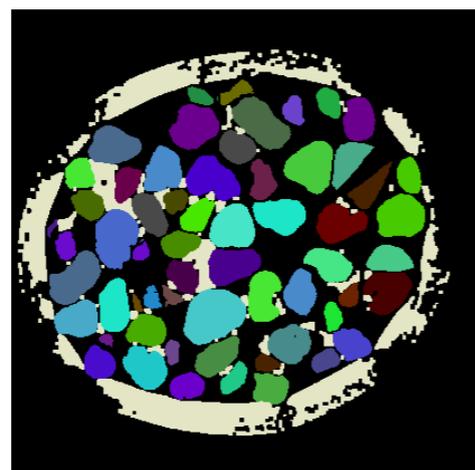
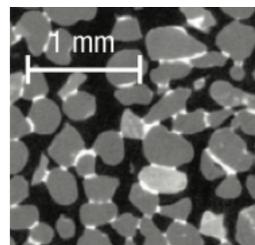
10.9% strain

Particles

Epoxy

3D volume correlation (DVC) – Example later

Can do this with water



Multi-phase segmentation

[Hurley, unpublished. Scheel, et al., Nature, 2008.]

In-situ XRCT images, resolutions to 0.3 μm

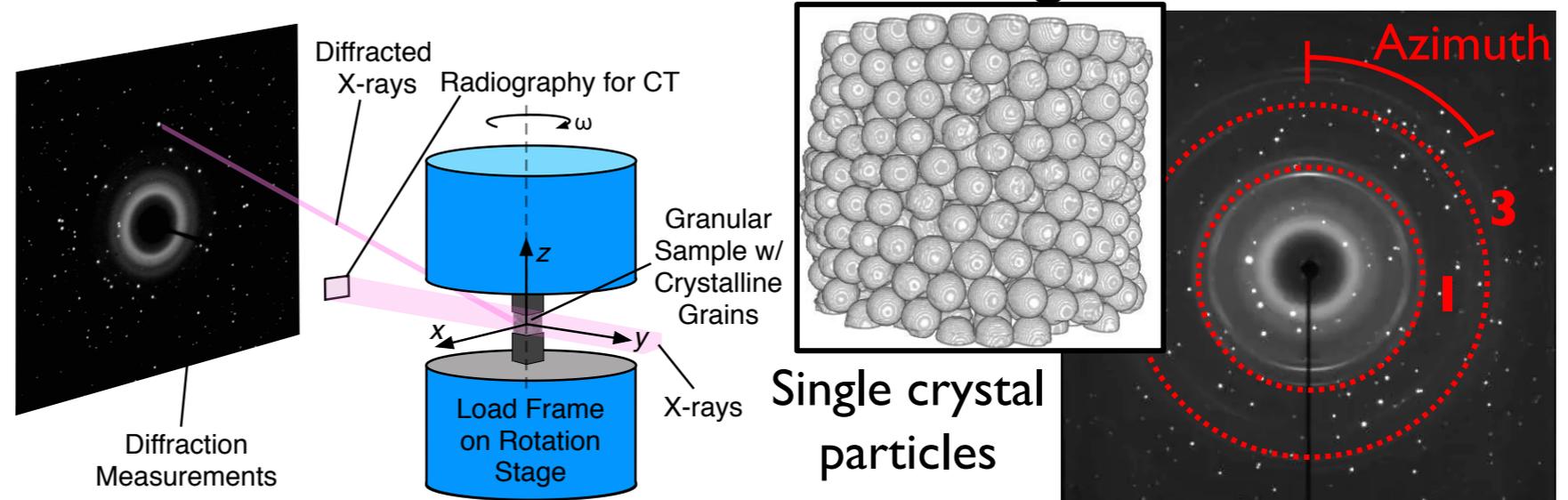
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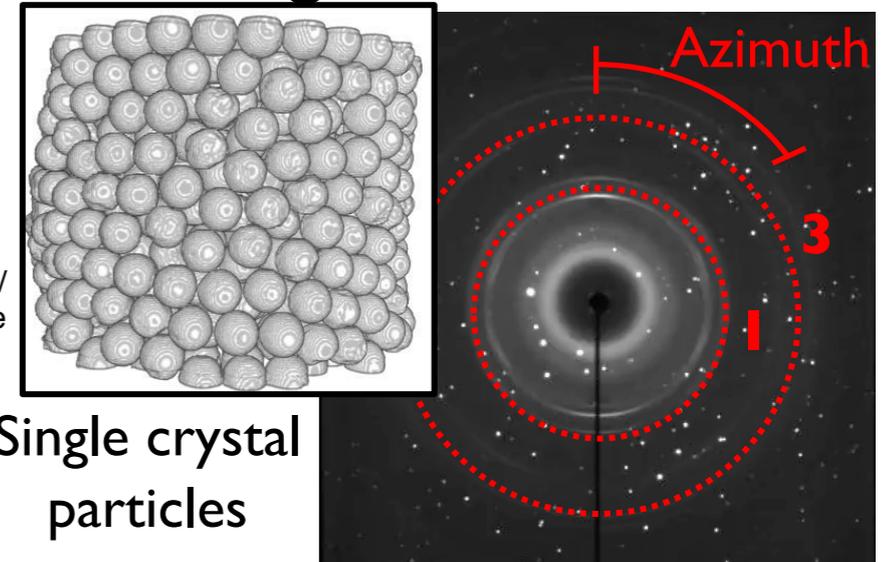
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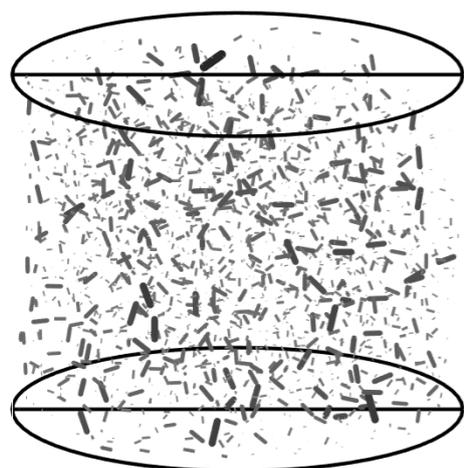
Advanced Photon Source (APS)



Experiment Schematic



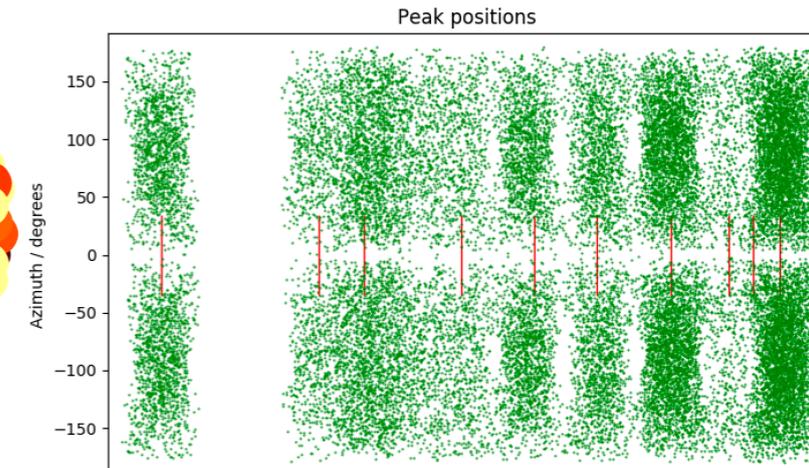
Bragg peaks with  $2\theta$ ,  $\omega$ , azimuth



Quantitative inter-particle force vectors at all contacts  
[Hurley, et al., PRL, 2016.]



$0^\circ$   $\Delta\theta$   $6^\circ$   $0$   $-\sigma_{ii}/3$  (MPa)  $75$

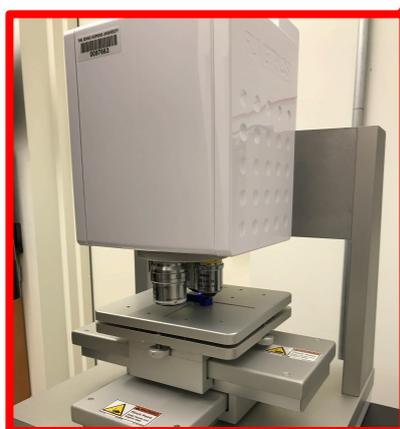


Peaks processed for strain tensors, orientations, positions

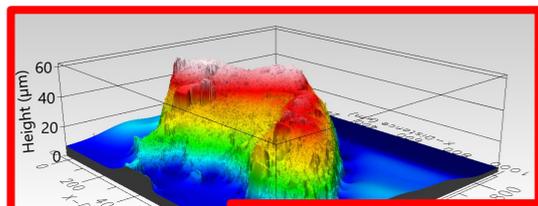


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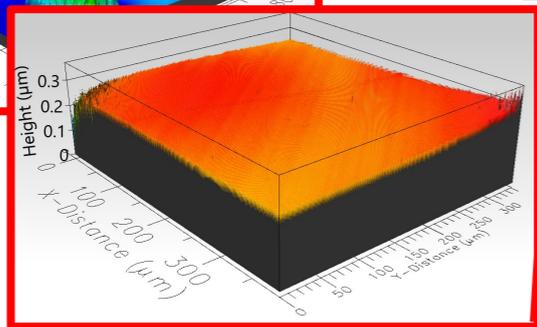
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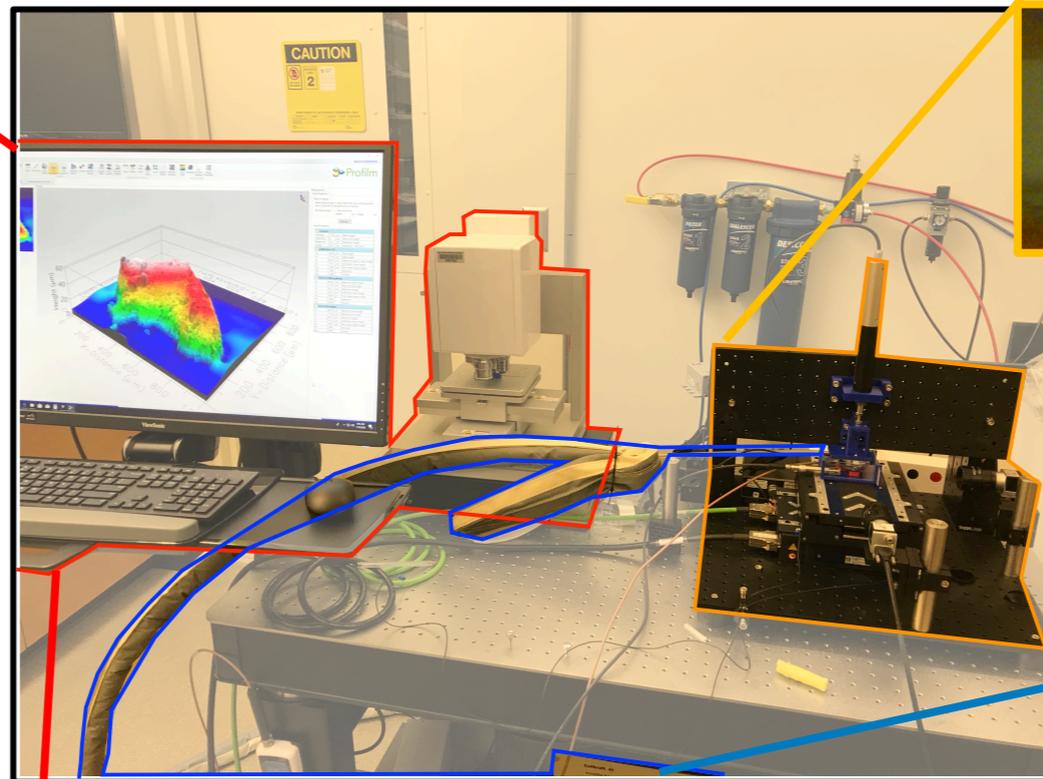
Profilm3D Profilometer, ~ 1 nm surface feature height



Ex: Ottawa sand

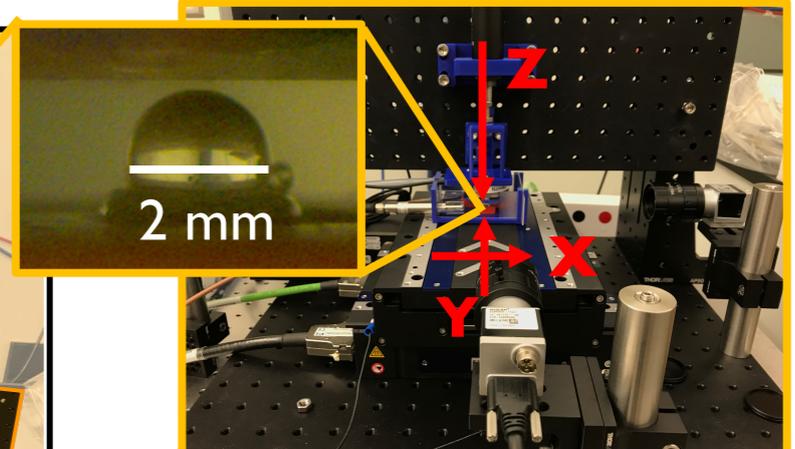
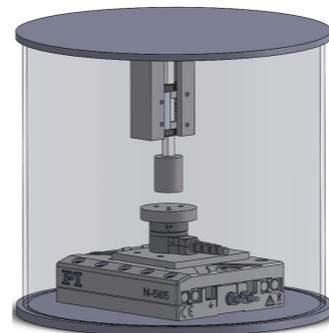


Ex: Quartz wafer



Surface and Contact Micromechanics Device at JHU

(Miniaturized version for X-ray nano-tomography, 3DXRD)

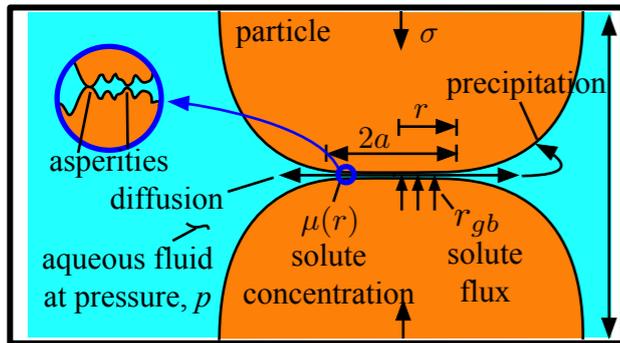


XYZ contact/shear tests. 1 nm XY, 50 nm Z, 6-axis load cell, forces down to 4  $\mu$ N

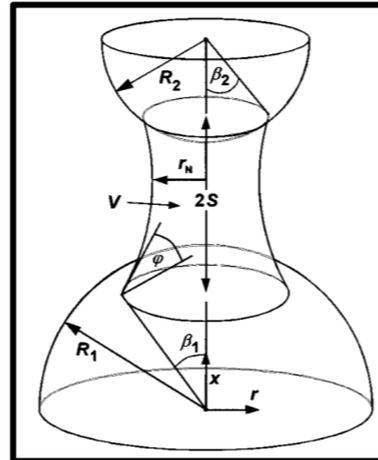


Humidifier: 0-100%, 0-50°C

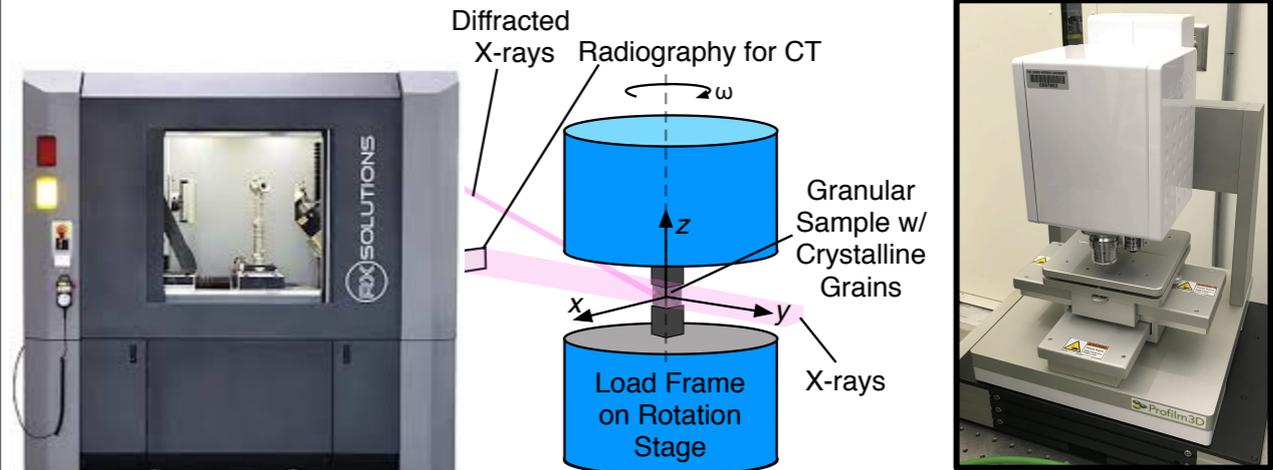
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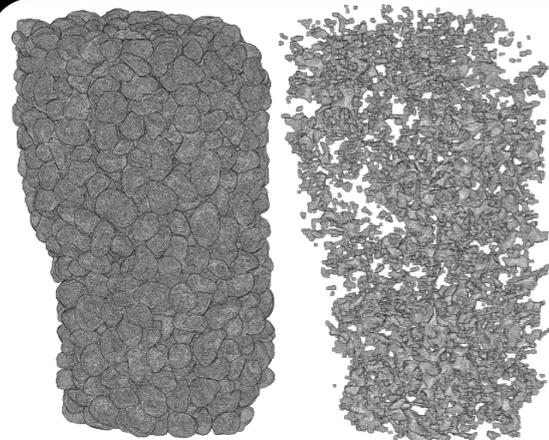
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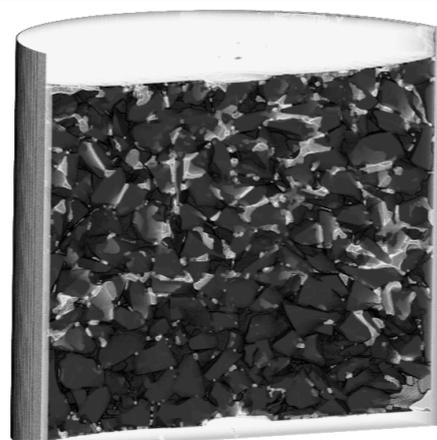
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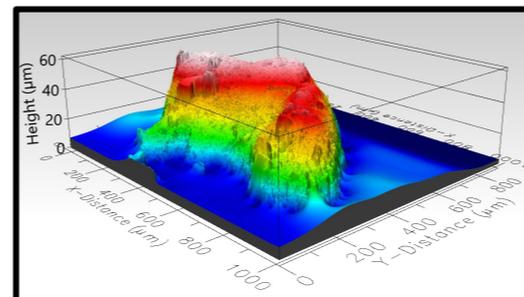
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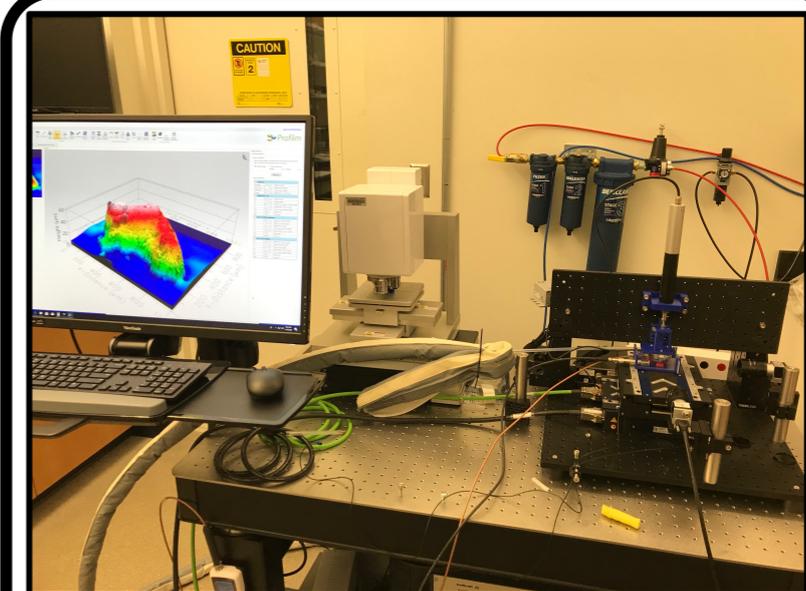
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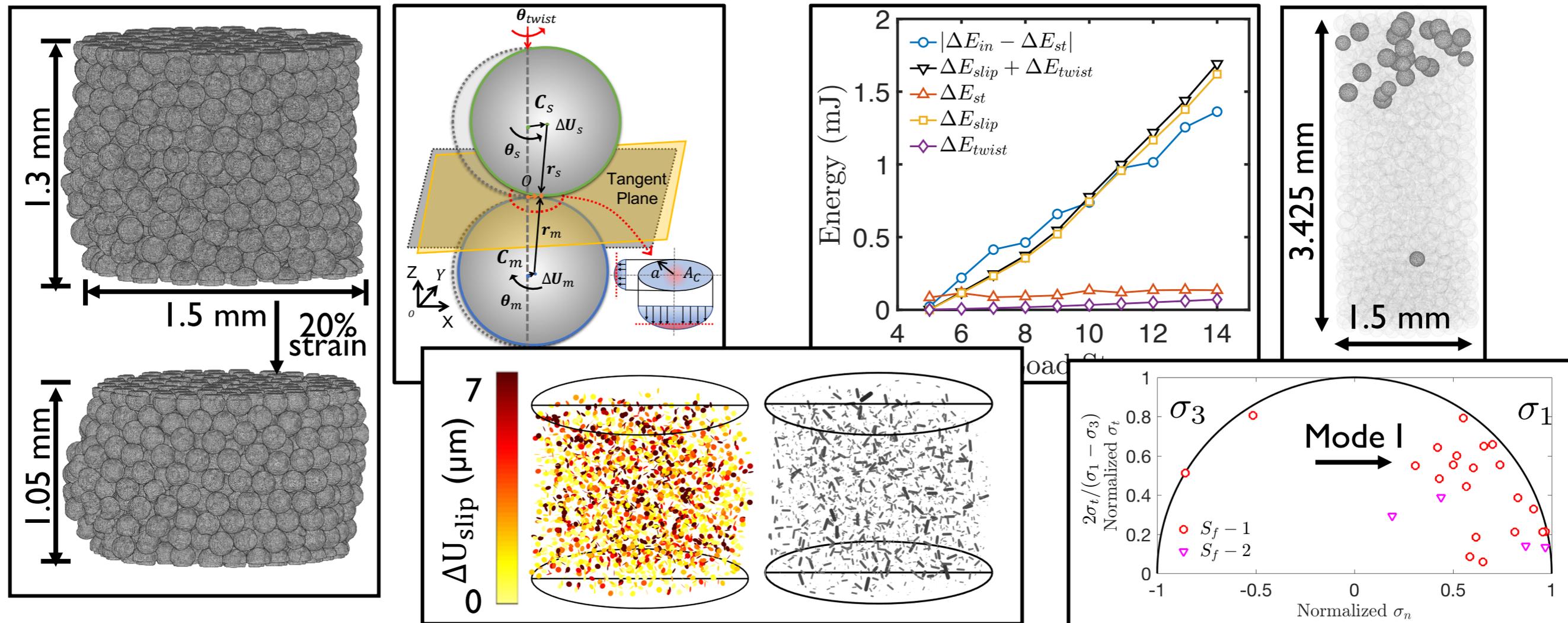
4. Summary, Goals

1. Mechanisms, Challenges

3. Past & Future Applications

# 3. Application (1/3): Cementation, XRCT

Addressing cementation challenges: (1) Link particle/binder props. and bulk elastic ( $E$ ,  $\nu$ ) and fracture ( $K$ ,  $G$ ) properties? (2) Particle/contact-scale fracture/fragmentation modes? (3) Non-uniform strain/stress fields?



We have developed tools for XRCT data that evaluate local kinematics & dissipation (and local particle stress fields using 3DXRD). **These are being used to address fracture modes in cemented materials.**

[Zhai, et al. *JMPS*, 2019. Hurley, et al., *PRL*, 2016. Hurley, et al., *J. Mech. Phys. Solids*, 2018.]

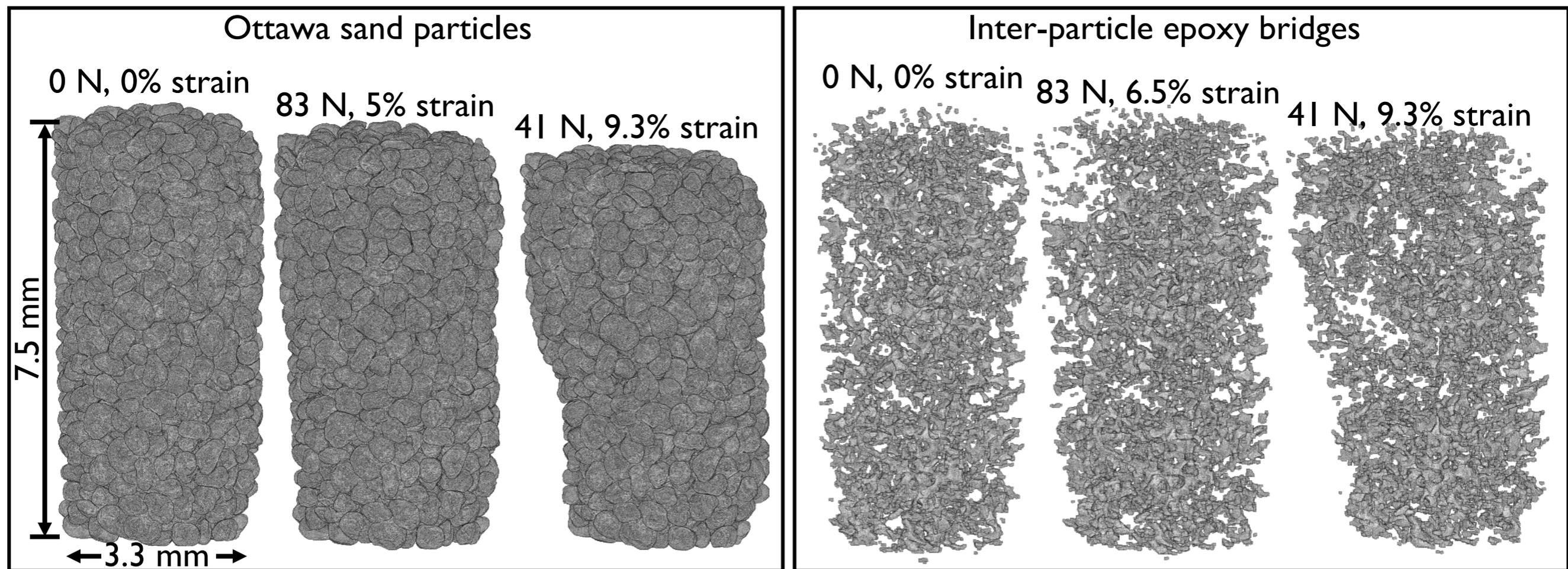
# 3. Application (1/3): Cementation, XRCT

Cohesive cementation: fracture ( $K$ ,  $G$ ) properties? (2) Particle/contact-scale fracture/fragmentation modes? (3) Non-uniform strain/stress fields?

Particles: 1,000 Ottawa (98%  $\text{SiO}_2$ ) sand particles, passing 300  $\mu\text{m}$  sieve

Sample: Sand mixed with 5% (by vol.) Extec epoxy, cured 24 hours

Loading: Uniaxial compression with 316  $\mu\text{m}$ -thick membrane

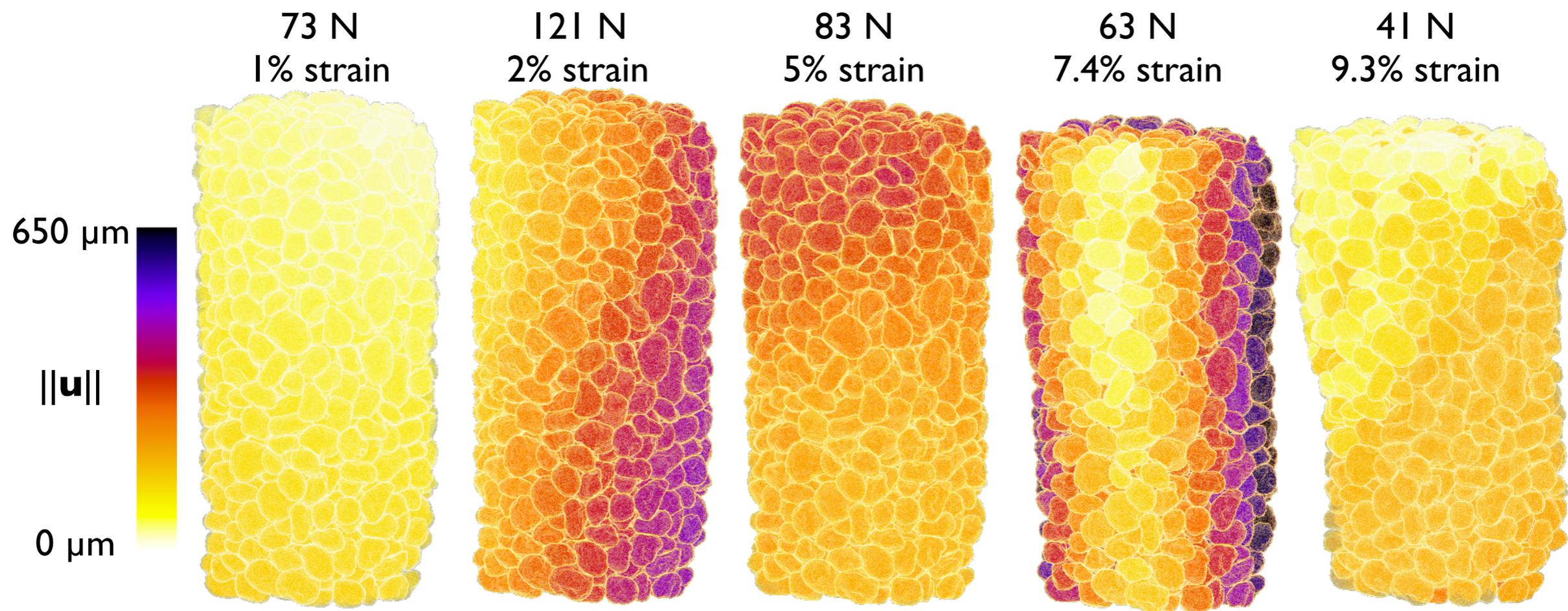


[Zhai & Hurley, unpublished, 2020.]

# 3. Application (1/3): Cementation, XRCT



Cohesive cementation: mechanisms of fragmentation – *in-situ* 3D DVC for particle kinematics, image analysis for particle/cement fracture



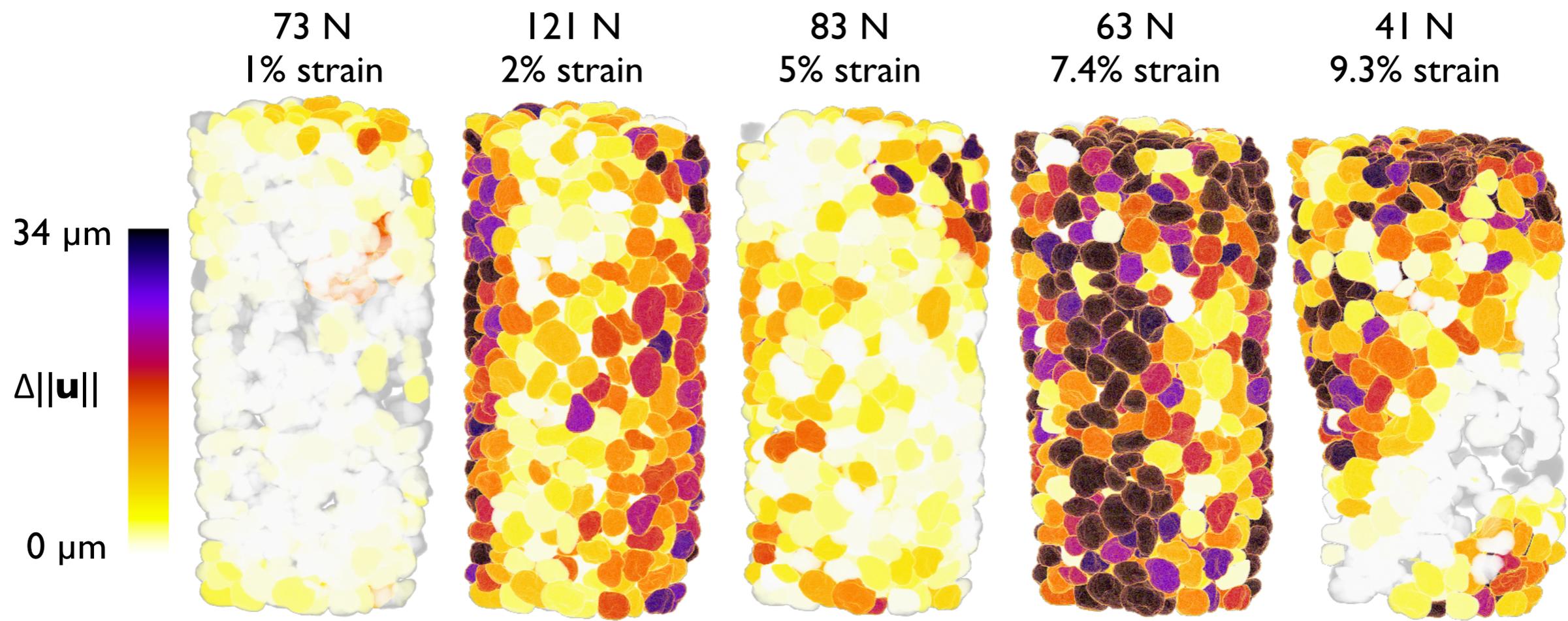
Total displacement of particles from 3D Discrete Digital Volume Correlation (3D-DVC).  
3D-DVC code is SPAM, partially developed with Lab 3SR, Grenoble.

[Zhai & Hurley, unpublished, 2020. DVC code: Ando, et al., unpublished]

# 3. Application (1/3): Cementation, XRCT



Cohesive cementation: mechanisms of fragmentation – *in-situ* 3D DVC for particle kinematics, image analysis for particle/cement fracture



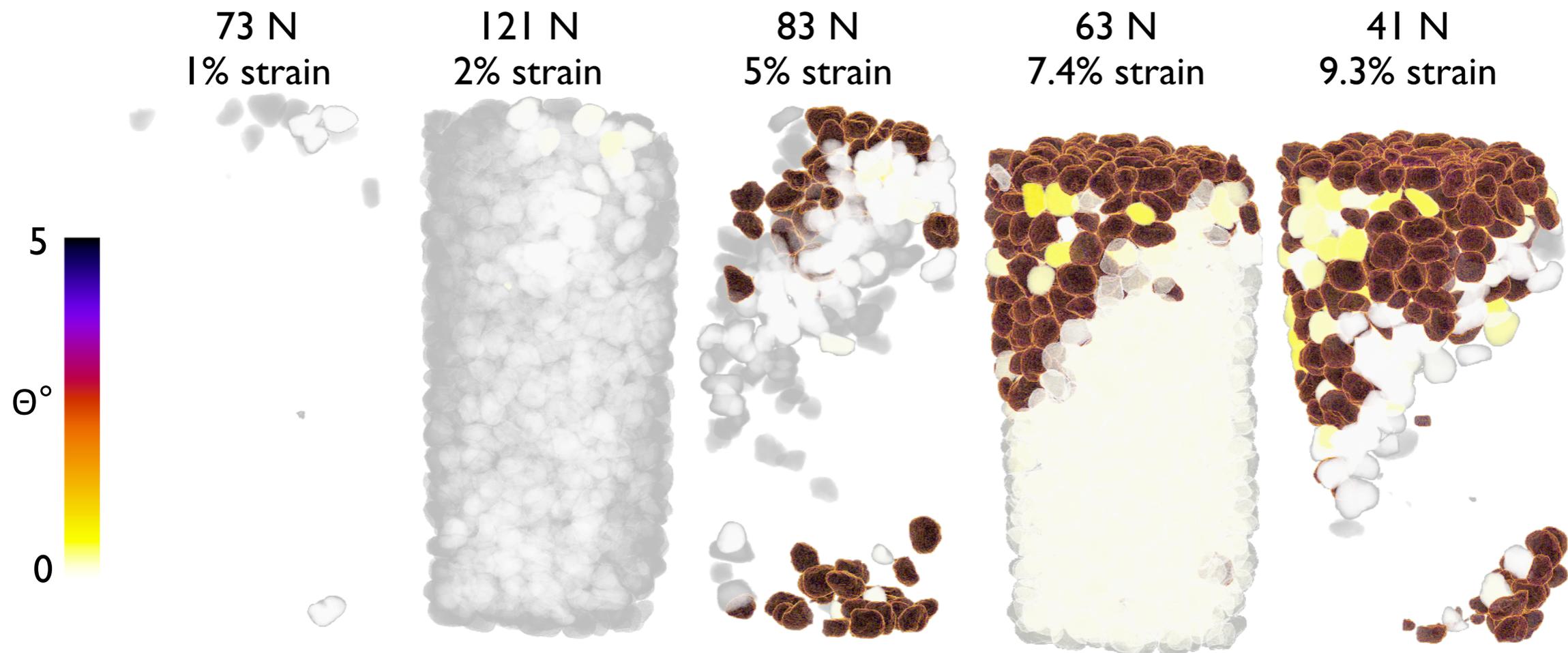
*Relative Displacements* of particles from their 15 nearest neighbors from 3D Discrete Digital Volume Correlation (3D-DVC)

[Zhai & Hurley, *unpublished*, 2020. DVC code: Ando, *et al.*, *unpublished*]

# 3. Application (1/3): Cementation, XRCT



Cohesive cementation: mechanisms of fragmentation – *in-situ* 3D DVC for particle kinematics, image analysis for particle/cement fracture



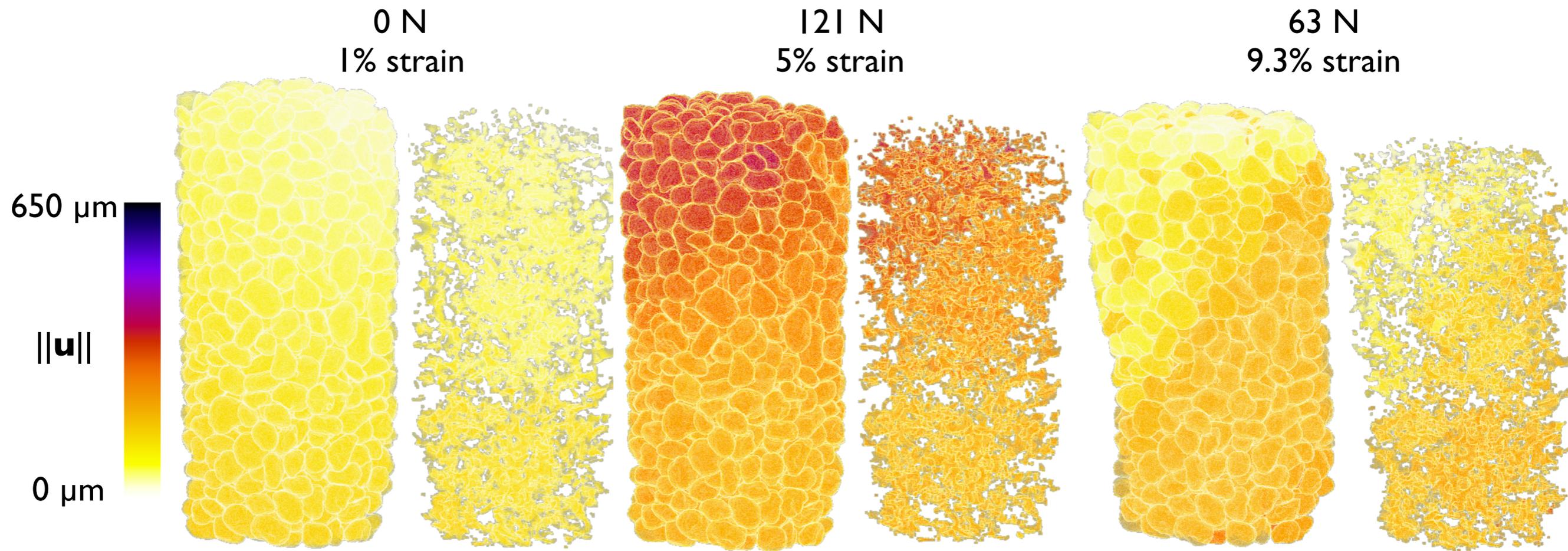
Rotations of individual particles from 3D Discrete Digital Volume Correlation (3D-DVC) [Note: fractured particles will appear to rotate more]

[Zhai & Hurley, *unpublished*, 2020. DVC code: Ando, *et al.*, *unpublished*]

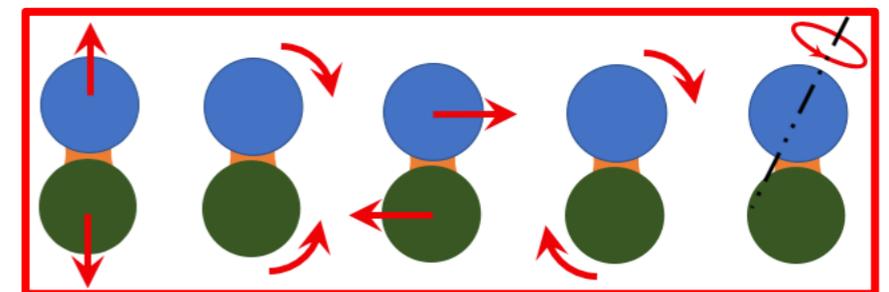
# 3. Application (1/3): Cementation, XRCT



Cohesive cementation: mechanisms of fragmentation – *in-situ* 3D DVC for particle kinematics, image analysis for particle/cement fracture



Total displacement of *both* particles and cement bridges can be used to quantify relative contribution of adhesive/cohesive/fracture modes to overall elastic and fracture properties of bulk.



Can evaluate at each contact

[Zhai & Hurley, *unpublished*, 2020. DVC code: Ando, *et al.*, *unpublished*]

# 3. Application (2/3): Cementation, 3DXRD

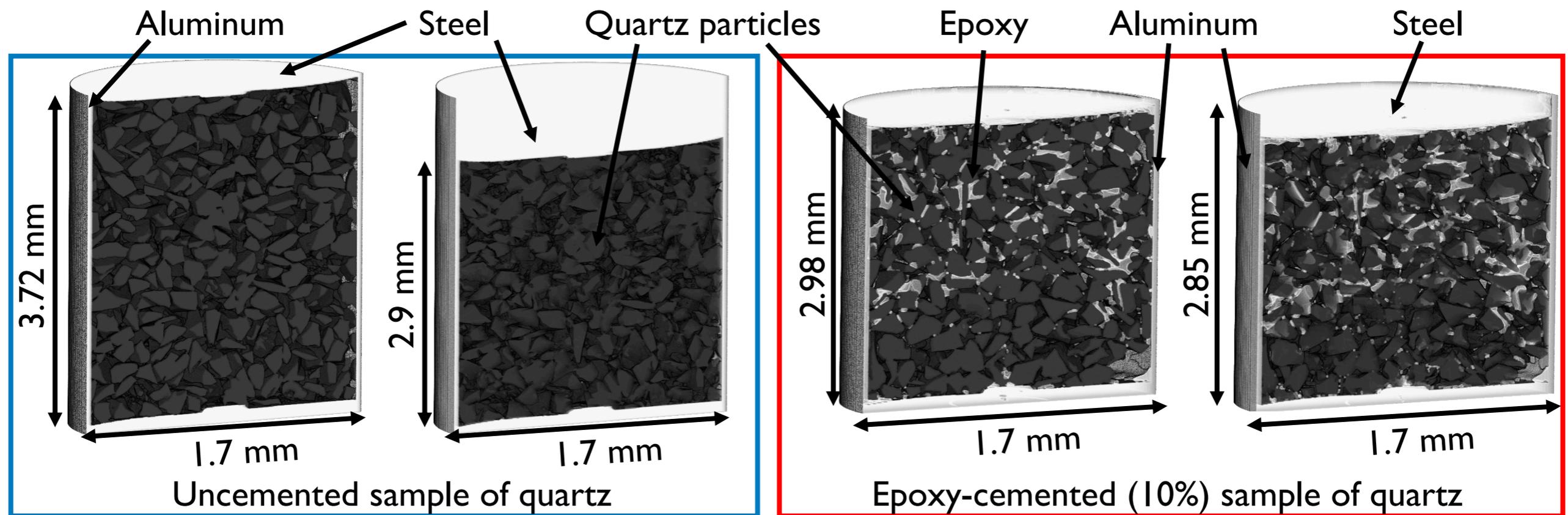


Cohesive cementation: fracture ( $K$ ,  $G$ ) properties? (2) Particle/contact-scale fracture/fragmentation modes? (3) Non-uniform strain/stress fields?

Particles: single-crystal quartz, ball milled, sieved between 150-277  $\mu\text{m}$

Sample 1: ~2,000 particles, 3.72 mm tall, 1.7 mm diam., strained to > 20%

Sample 2: ~1,700 particles, 2.98 mm tall, 1.7 mm diam., strained to > 4%

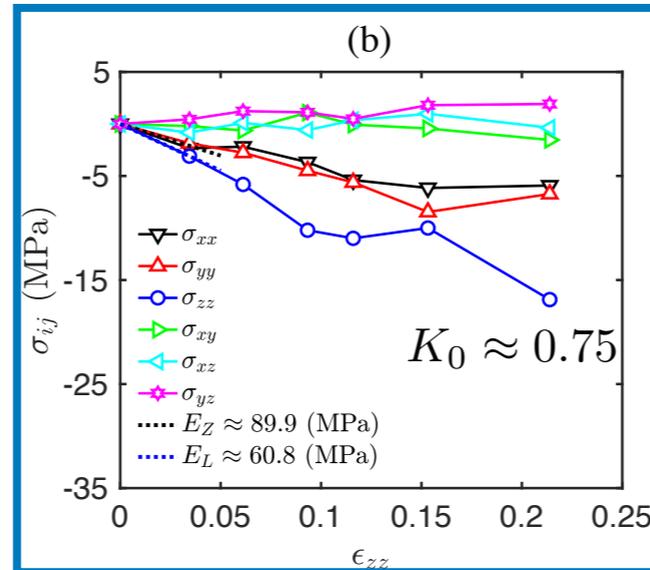
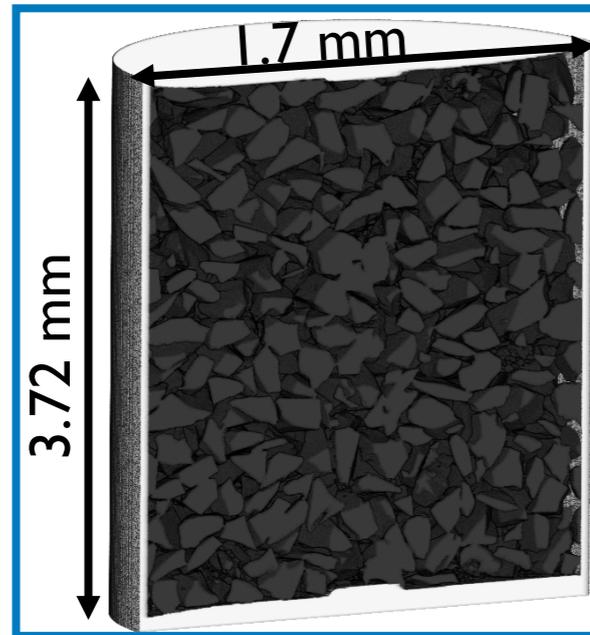


[Zhai, et al., JOM, 2020.]

# 3. Application (2/3): Cementation, 3DXRD



Comparison of bulk behavior: epoxy-cemented sample is stiffer, has a lower  $K_0$  (proportionality) value (ratio of lateral to axial stress)



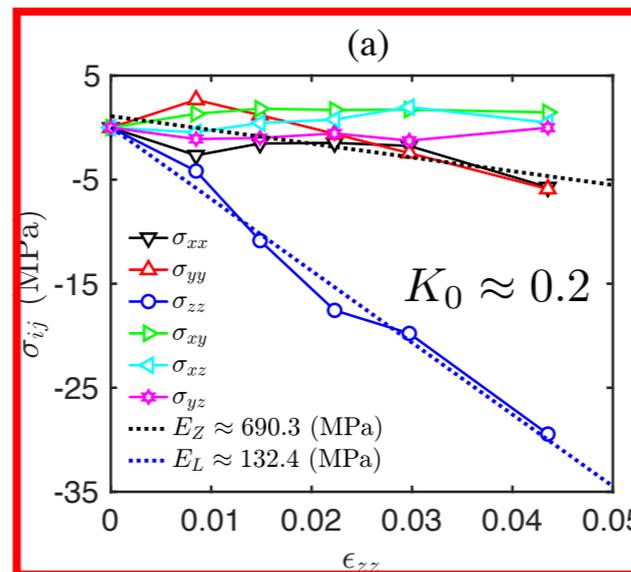
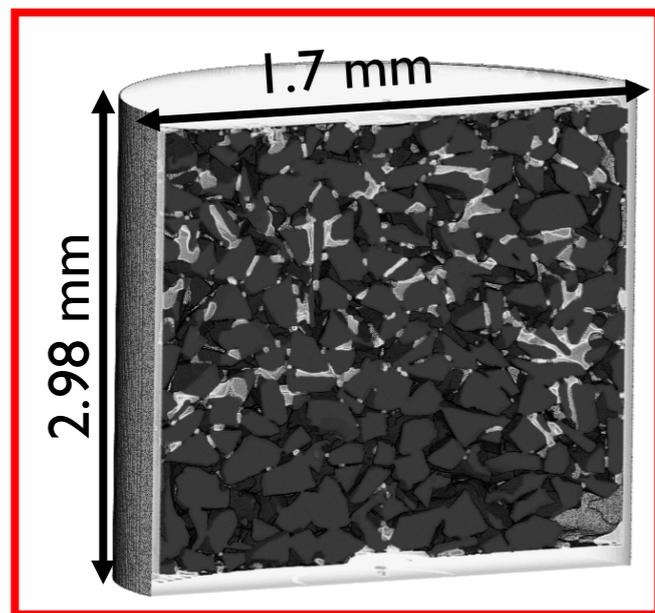
Uncemented sample

$$E_Z = 89.9 \text{ MPa}$$

$$E_L = 60.8 \text{ MPa}$$

$$K_0 = 0.75$$

Dramatic shift in elastic properties with 10% binder



Epoxy-cemented sample

$$E_Z = 690.3 \text{ MPa}$$

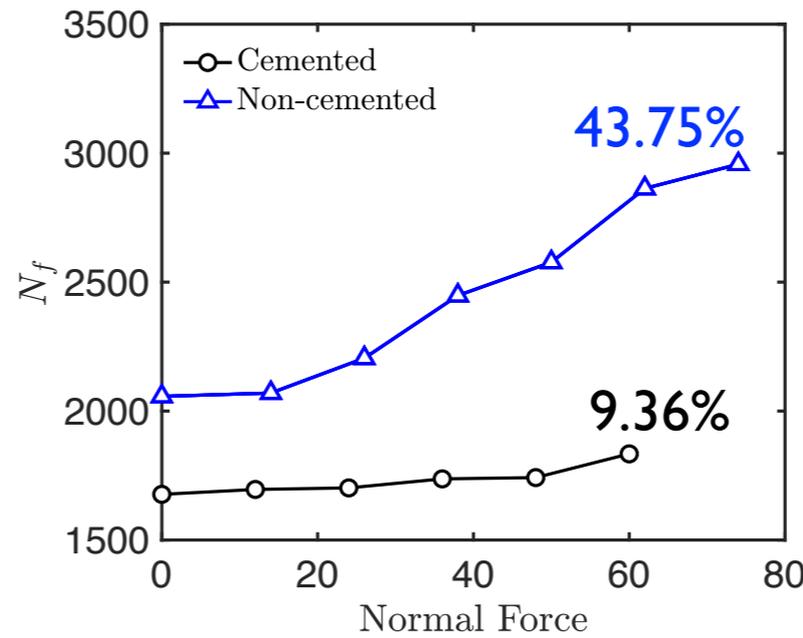
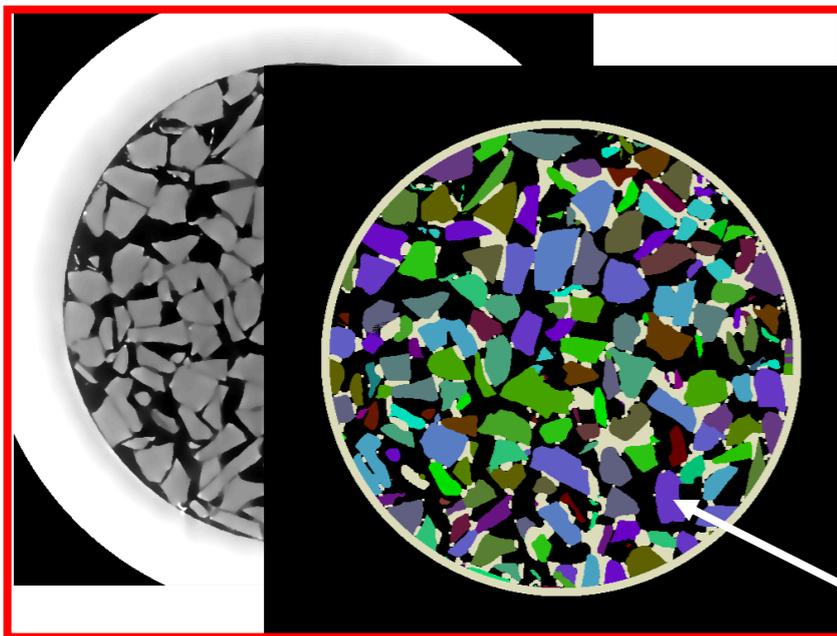
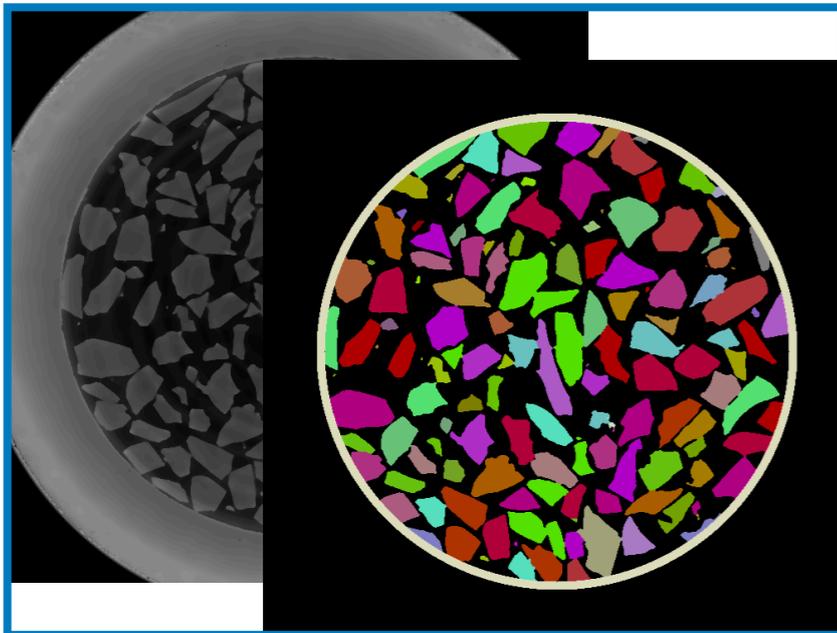
$$E_L = 132.4 \text{ MPa}$$

$$K_0 = 0.2$$

[Zhai, et al., JOM, 2020.]

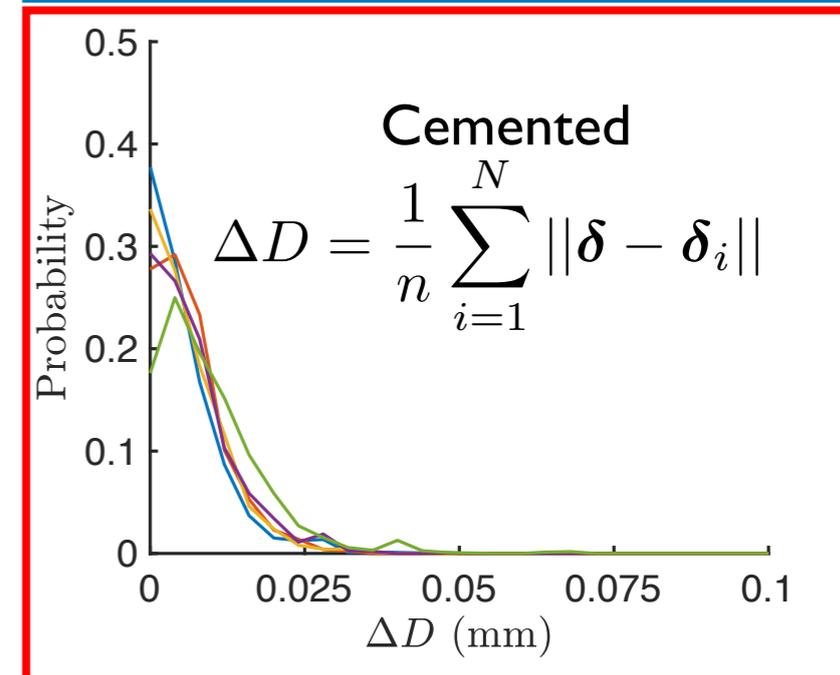
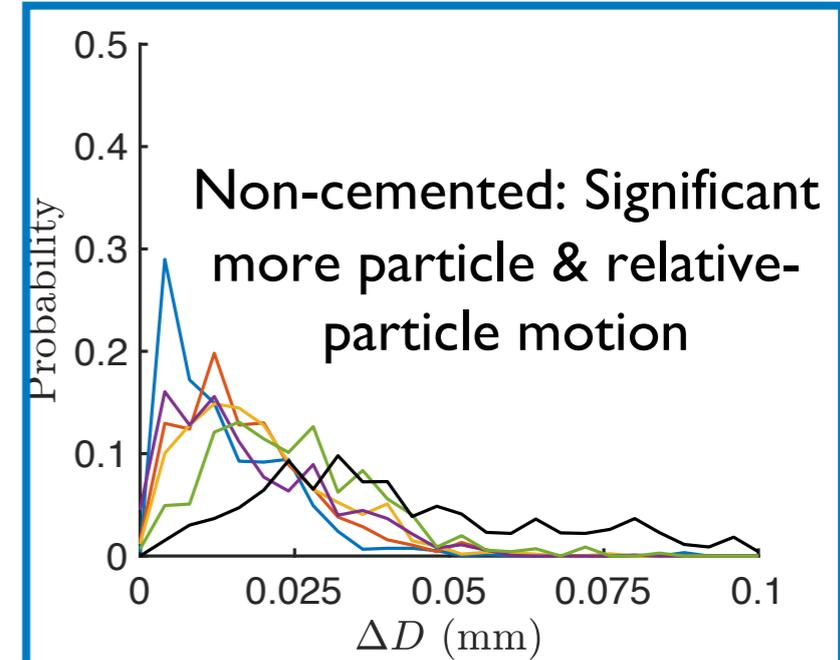
# 3. Application (2/3): Cementation, 3DXRD

Microstructural characterization: XRCT allows particle, cement-bridge segmentation (via MATLAB or SPAM), analysis of fragmentation, kinematics



Significantly more fragmentation in non-cemented sample

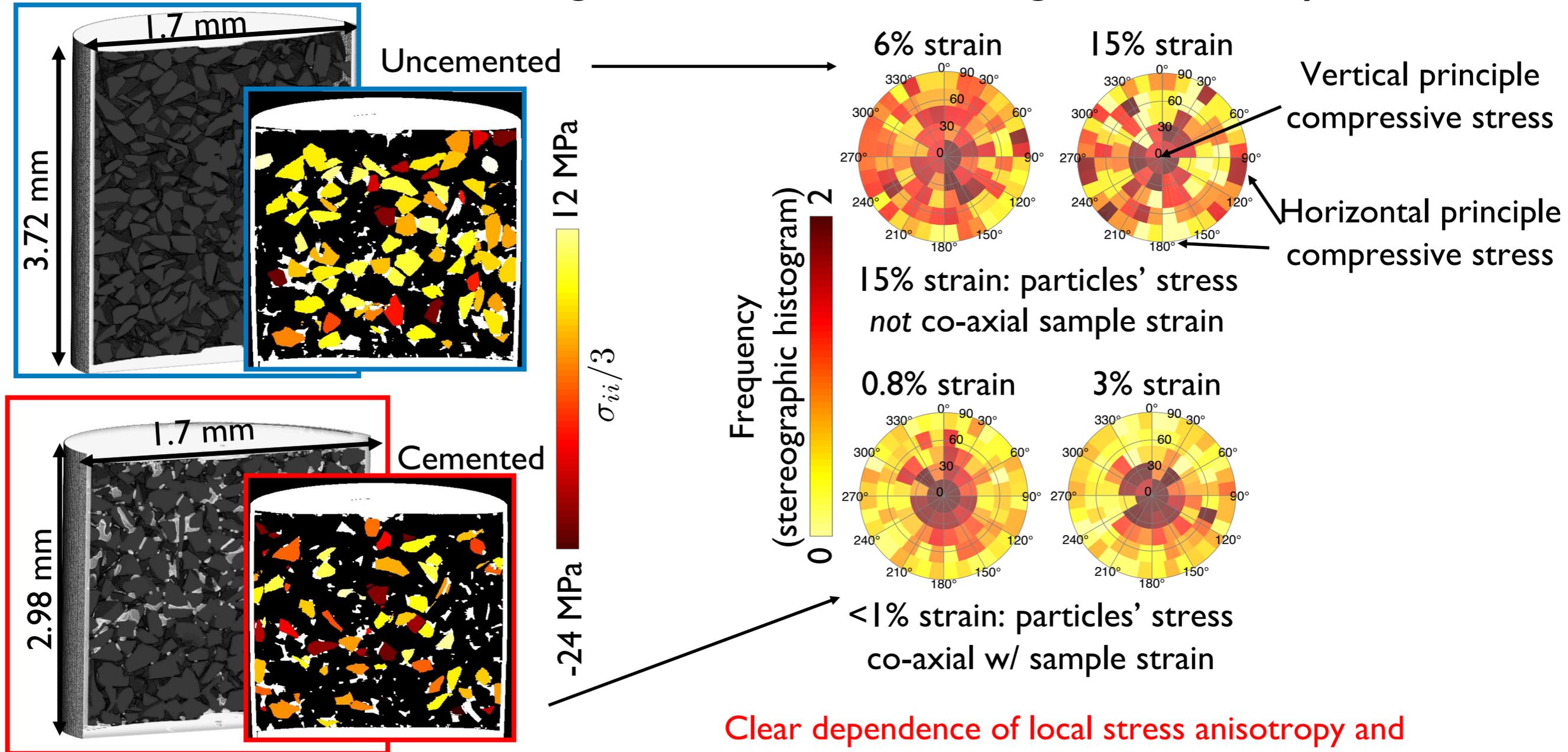
Each with unique label



[Zhai, et al., JOM, 2020.]

# 3. Application (2/3): Cementation, 3DXRD

Microstructural characterization: 3DXRD allows calculation of intra-particle stress tensors and assessing local stresses vs bridges, co-axiality, etc.



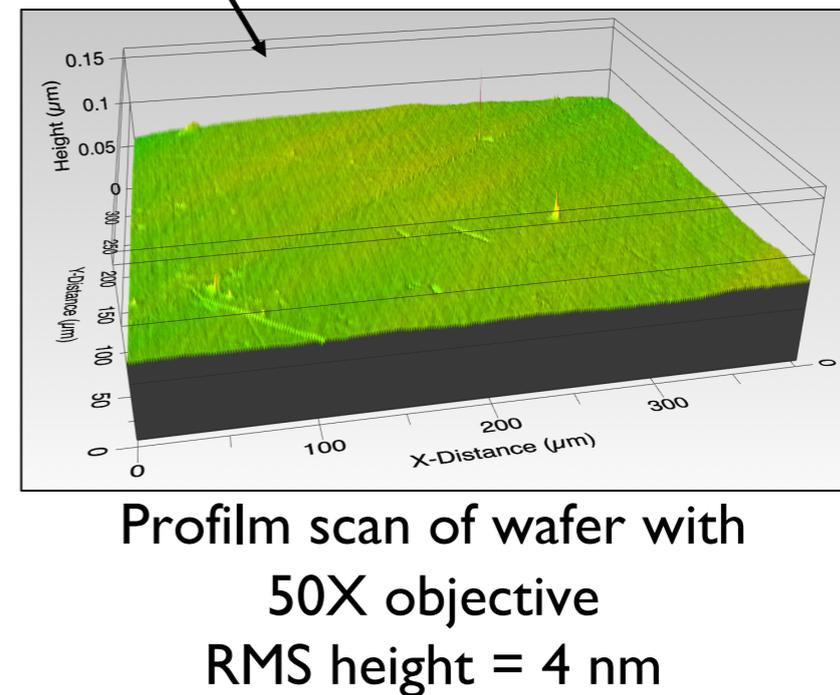
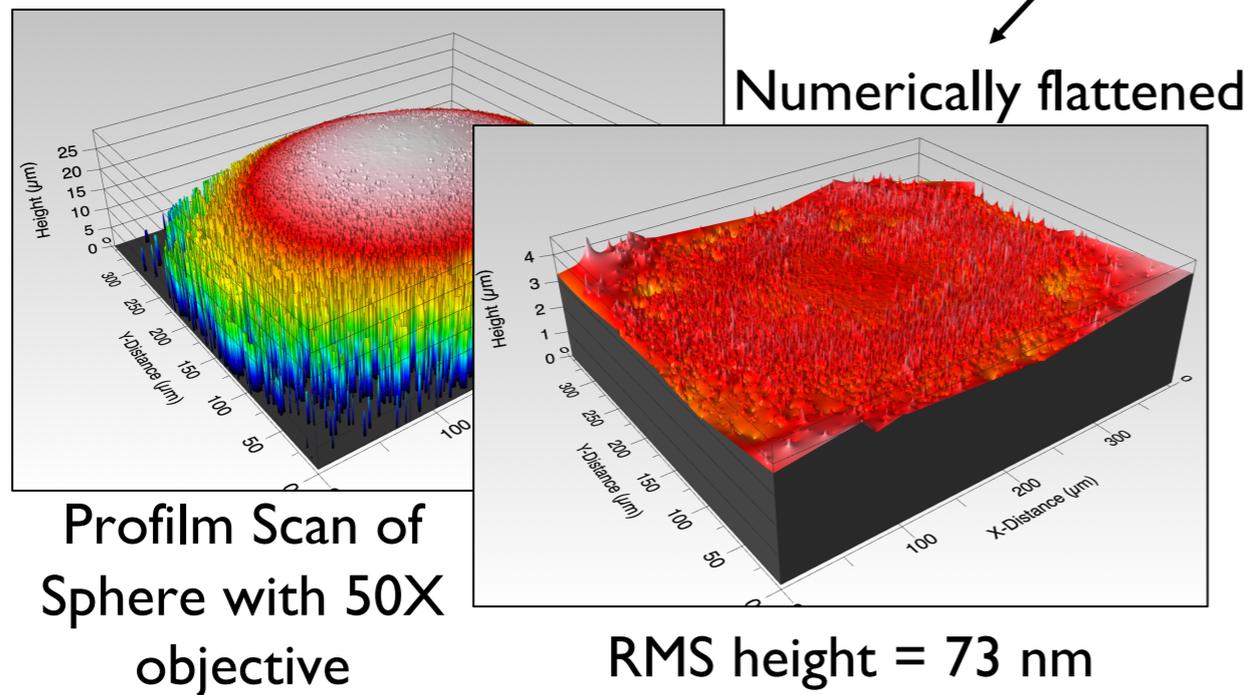
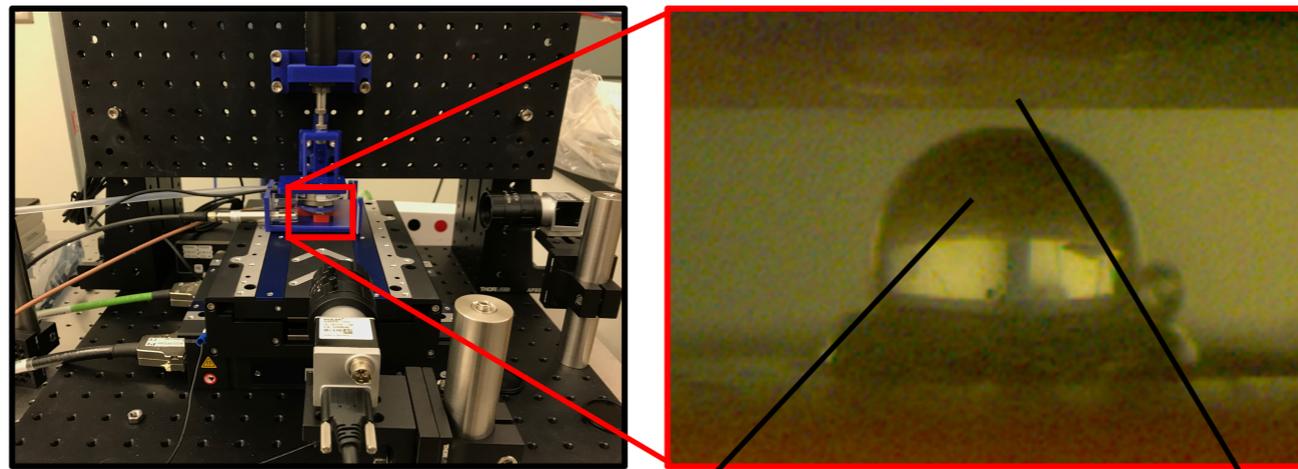
Clear dependence of local stress anisotropy and homogeneity with cementation. Can also look at force chains as a function of cementation.

[Zhai, et al., JOM, 2020.]

# 3. Application (3/3): Humidity & Roughness

Addressing humidity/roughness: (I) Adhesion and friction forces as a function of humidity & roughness at both contact- and bulk scales?

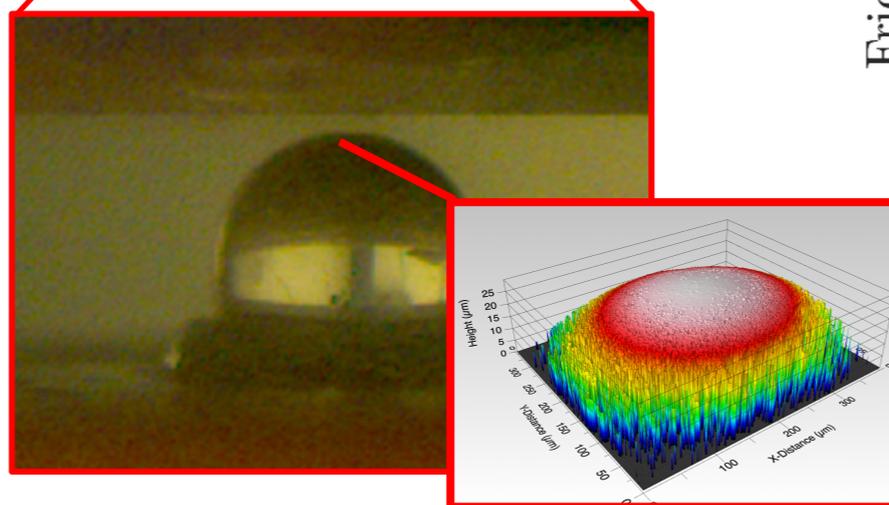
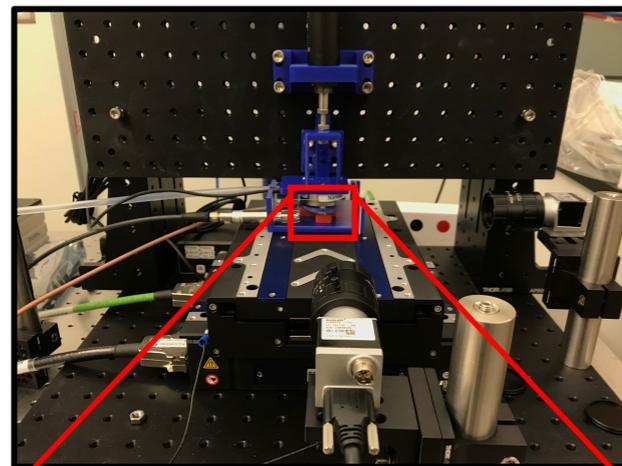
Test I: compression and sliding of 2 mm borosilicate sphere on a quartz wafer at 35%, 55%, 75% relative humidity



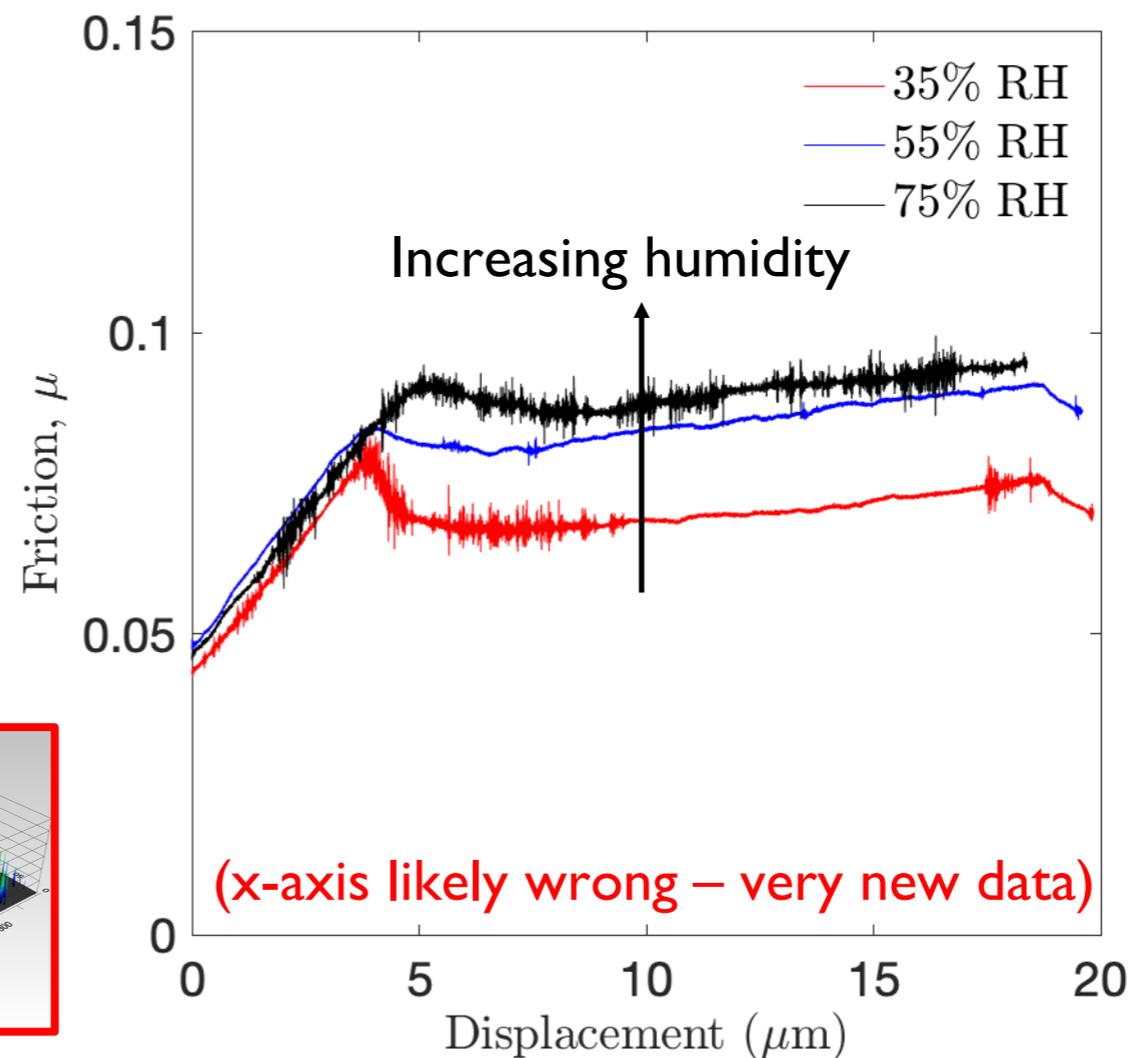
# 3. Application (3/3): Humidity & Roughness

Addressing humidity/roughness: (I) Adhesion and friction forces as a function of humidity & roughness at both contact- and bulk scales?

Test I: compression and sliding of 2 mm borosilicate sphere on a quartz wafer at 35%, 55%, 75% relative humidity



RMS height = 73 nm

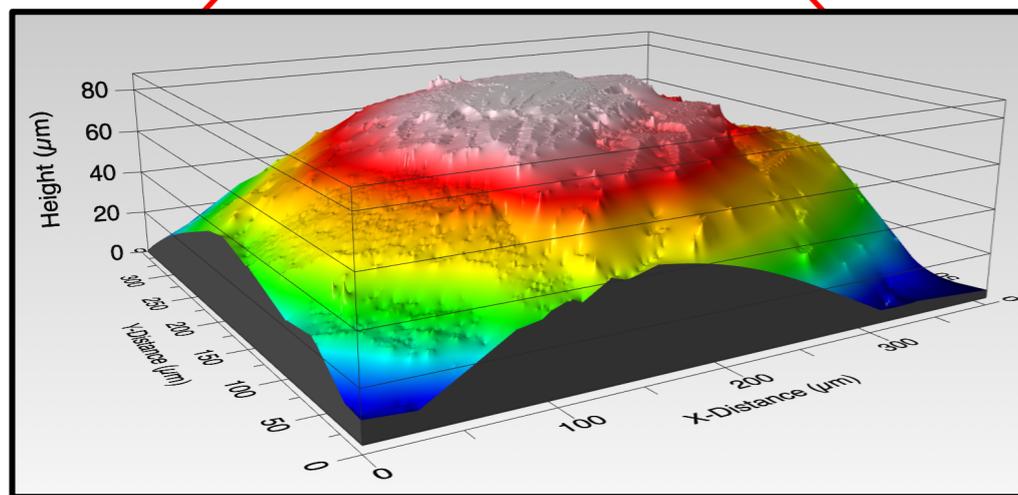
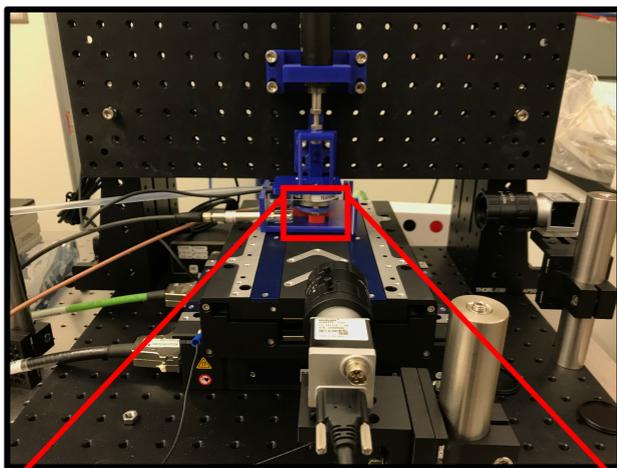


Compression followed by shear shows minor but clear humidity dependence at 4 N compressive

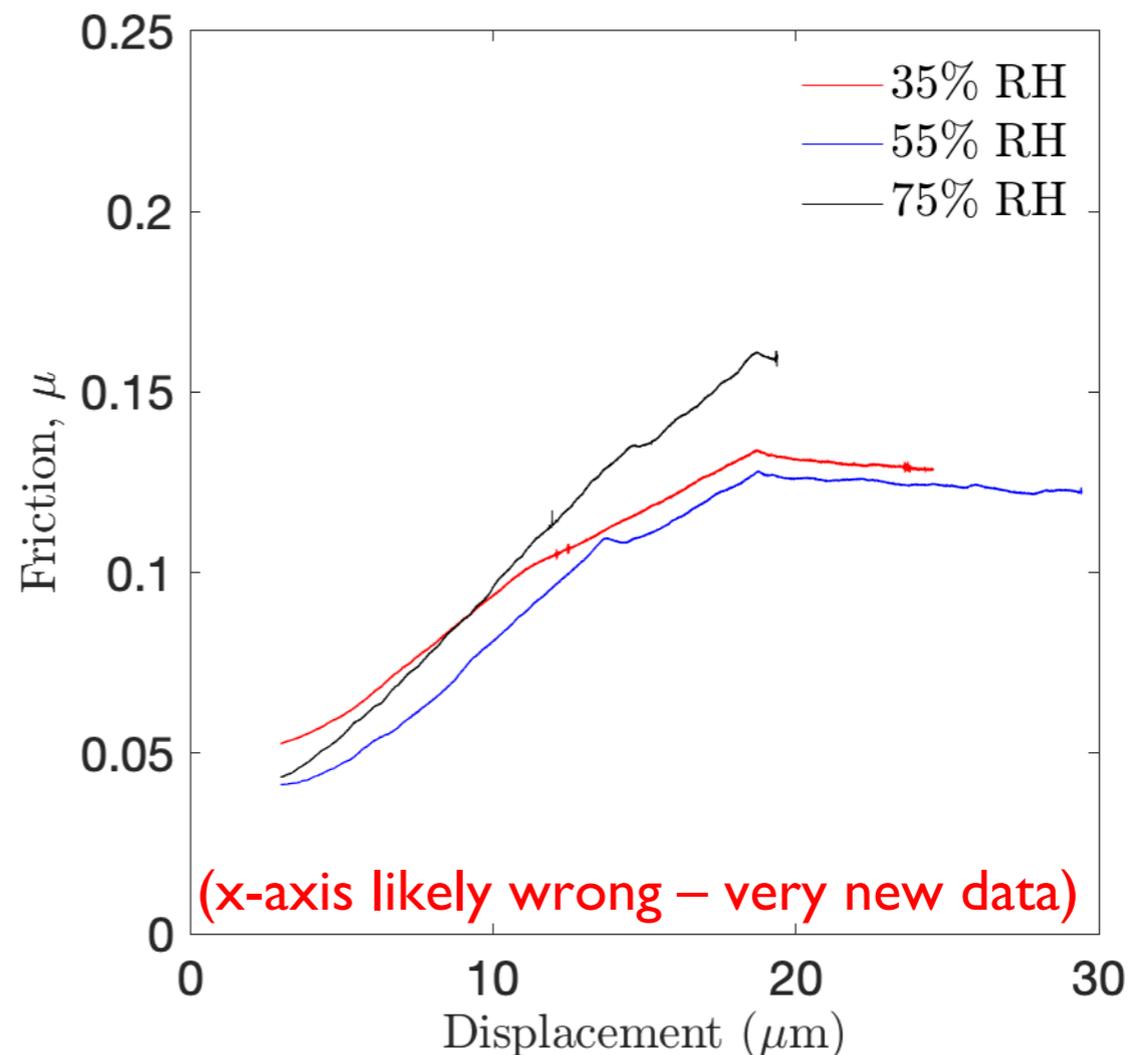
# 3. Application (3/3): Humidity & Roughness

Addressing humidity/roughness: (I) Adhesion and friction forces as a function of humidity & roughness at both contact- and bulk scales?

Test 2: compression and sliding of 0.8 mm Ottawa sand particle on a quartz wafer at 35%, 55%, 75% relative humidity

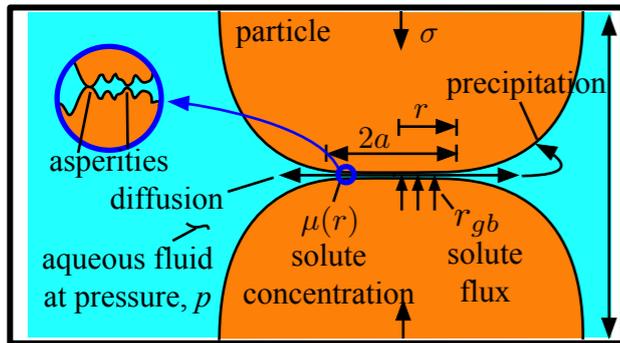


RMS height on contact: 1.067 μm

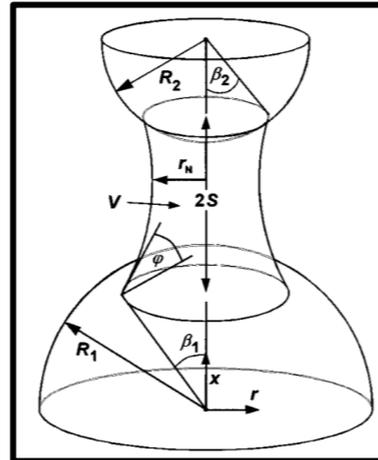


Compression followed by shear shows minimal and mixed humidity dependence at 4 N compressive

# Outline

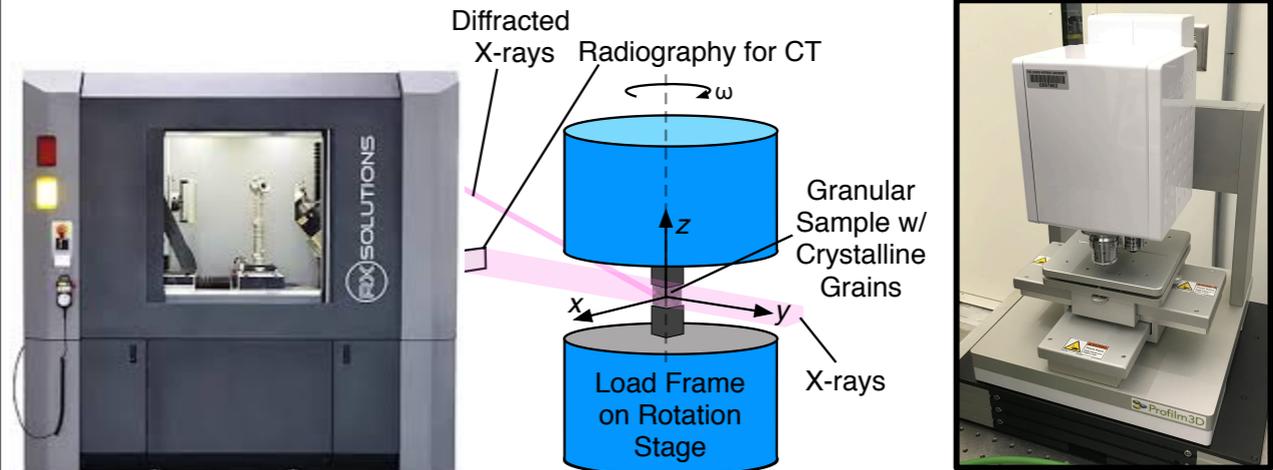


Inter-particle cementation

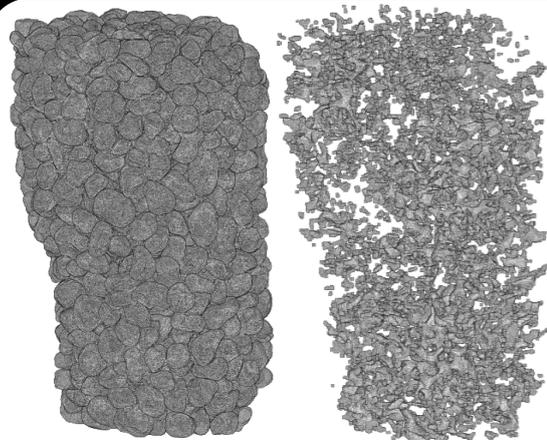


Capillary condensation

## 1. Mechanisms, Challenges



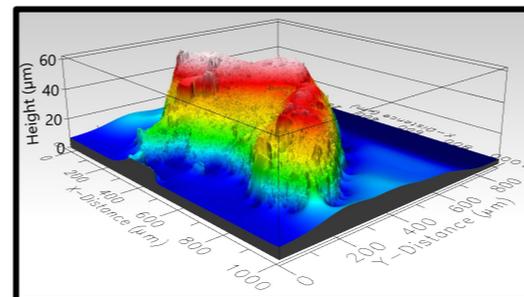
## 2. Characterization Tools



(1) XRCT: cemented cohesive mechanics

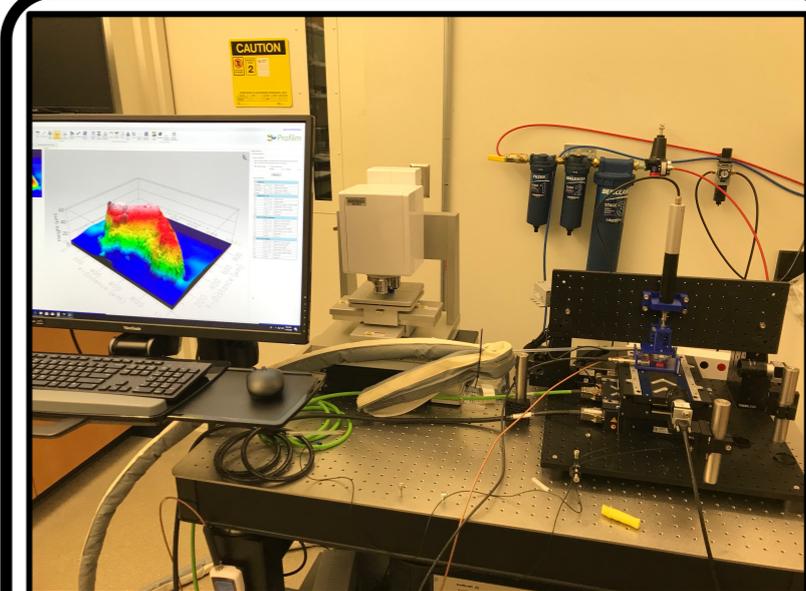


(2) XRCT + 3DXRD: particle-level stresses



(3) Roughness, %RH effects on particle-scale interactions

## 3. Past & Future Applications



## 4. Summary, Goals

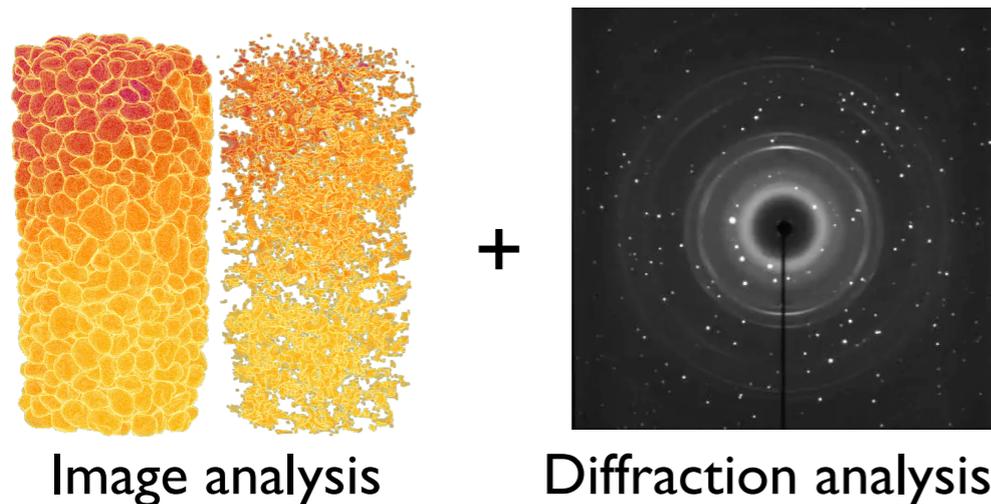


# 4. Summary

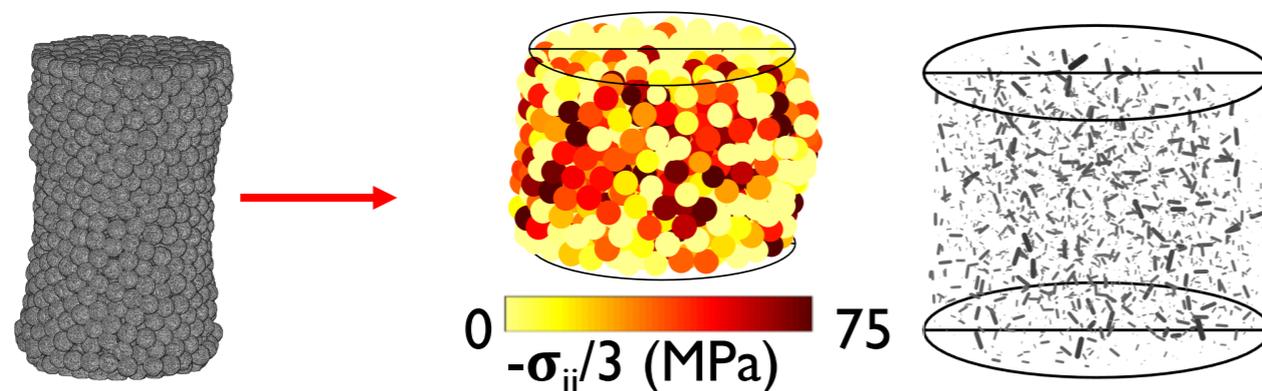
## Where are we going next?

### Cementation:

- Using XRCT & 3DXRD, we are developing tools to **quantify microscale contributions to elastic & fracture properties of cemented granular media.**

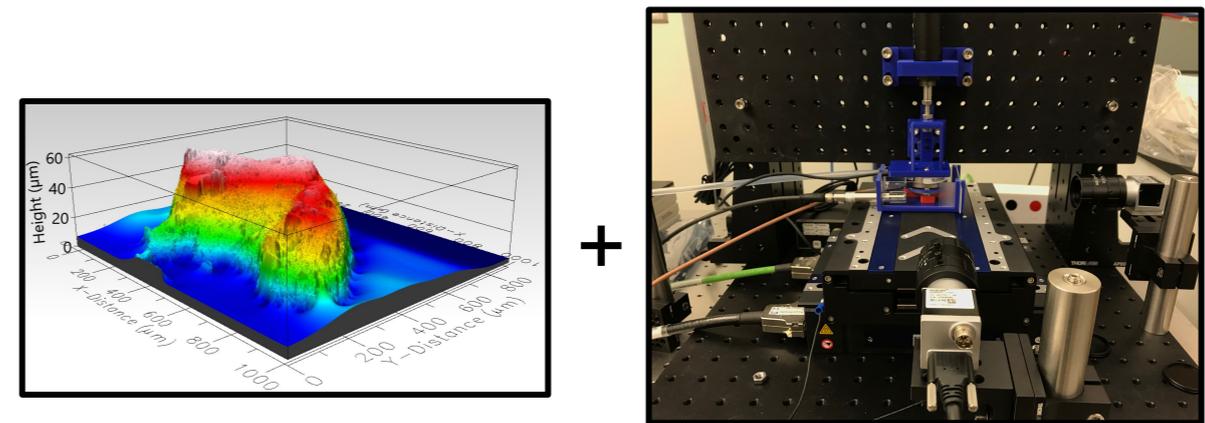


- Upcoming synchrotron experiments (Feb 2020): **XRCT & 3DXRD to quantify microscopic contributions to failure in cemented materials.**

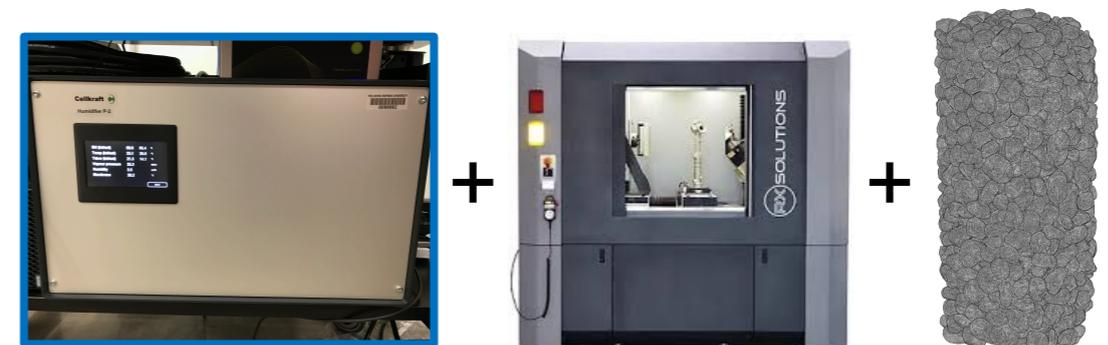


### Humidity/roughness:

- A new capability for surface structure analysis (profilometry) and in-situ contact (friction/adhesion) testing at any humidity will elucidate cohesion mechanisms across scales.**



- Future work may combine contact-scale with bulk-scale 3D XRCT studies of humid powders.**



# Thank you!



ARO DURIP Award



CHESS



Johns Hopkins  
University

**Ryan C. Hurley<sup>1</sup>**

<sup>1</sup>Mechanical Engineering, Hopkins Extreme Materials Institute, Johns Hopkins University

Thanks to: Chongpu Zhai, Postdoc  
Hopkins Extreme Materials Institute, Johns Hopkins University

